

# *(High field) Transport properties of strongly correlated metals*

***Cyril PROUST***

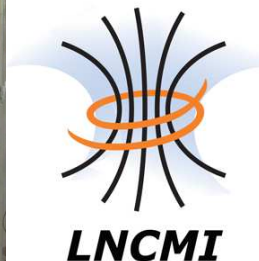
*Laboratoire National des Champs Magnétiques Intenses*

*Toulouse, France*



<http://www.lncmi.cnrs.fr>

<http://www.emfl.eu>



# Outline

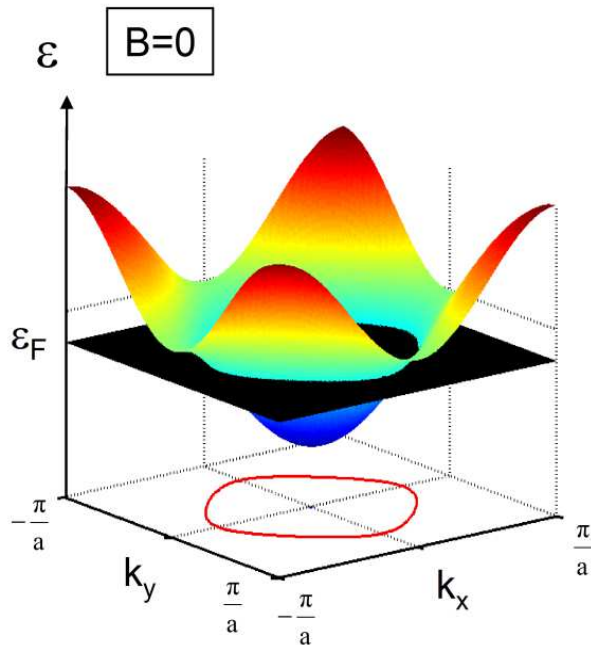
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1. Definitions & Reminders
2. Experimental techniques
3. Transport properties of SCES
4. High field transport measurements

# *1. Definitions & Reminders*

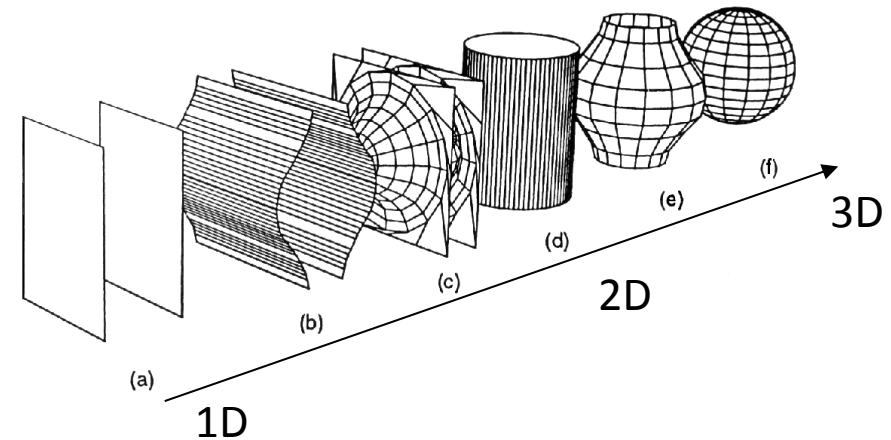
# Reminders

Band theory at 2D:  $\varepsilon(\vec{k}) = -2t(\cos(k_x a) + \cos(k_y b))$

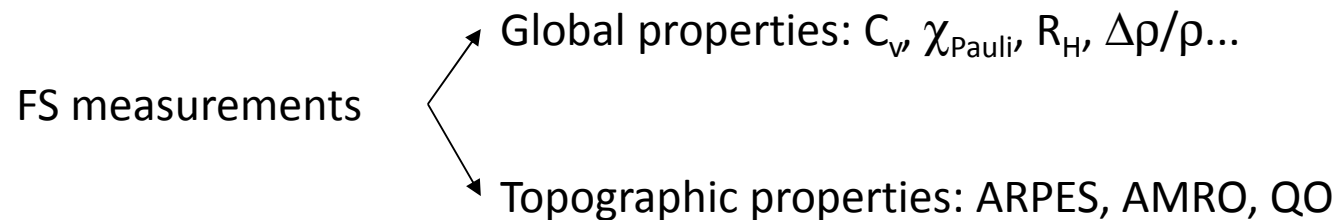


$\varepsilon_F \sim 1-10 \text{ eV}$

Typical excitations ( $\Delta V, \Delta T$ )  $\sim \text{meV}$



Comparison with band structure calculations, effect of interactions, phase transitions...



# Reminders

## Global properties

- Specific heat

$$C_v = \frac{\partial U}{\partial T} = \frac{\pi^2}{3} k_B g(\epsilon_F) \times T \quad \text{where} \quad U = \int_0^{E_F} \epsilon n(\epsilon) f(\epsilon) d\epsilon$$

$$g(\epsilon_F) = \frac{m^* k_F}{\hbar^2 \pi^2}$$

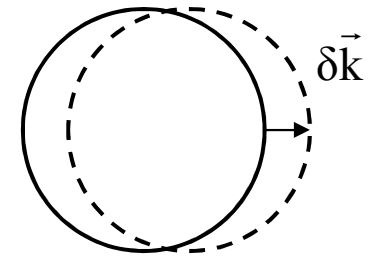
- Hall effect

$$R_H = \frac{\rho_{xy}}{B} = \frac{1}{nq}$$

- Magnetoresistance

$$\vec{J} = ne\vec{v} = e \int_{SF} \vec{v} \frac{\delta\vec{k} \cdot d\vec{S}}{4\pi^2} \quad \text{where} \quad \delta\vec{k} = \frac{e\tau}{\hbar} \vec{E}$$

$$\vec{J} = \frac{e^2 \tau}{4\pi^3 \hbar} \int_{SF} \vec{v} \cdot d\vec{S} \vec{E}$$



# Reminders

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## **Drude theory**

*Electrical conductivity*  $\sigma = \frac{ne^2\tau}{m^*} \quad [\Omega \text{ cm}]^{-1}$

*Thermal conductivity*  $\kappa = \frac{1}{3}v_F^2\tau C_v = \frac{1}{3}\ell v_F C_v \quad [\text{W} / \text{K cm}]$

*Wiedemann-Franz law:*  $\frac{\kappa}{\sigma} = \frac{\frac{1}{3}m^*v_F^2 C_v}{ne^2}$

if  $C_v = \frac{3}{2}nk_B$  and  $\frac{1}{2}m^*v_F^2 = \frac{3}{2}nk_B$

$$\frac{\kappa}{\sigma} = \frac{3}{2} \left( \frac{k_B}{e} \right)^2 T$$

$$\lim_{T \rightarrow 0} \frac{\kappa}{T\sigma} = L_0 \quad \text{where} \quad L_0 = \frac{\pi^2}{3} \left( \frac{k_B}{e} \right)^2$$

Universal law, i.e. robust signature of Fermi liquid theory, stating that the electronic carriers of heat are fermionic excitations of charge  $e$ .

# Reminders

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## ***Boltzmann theory***

$f_k(r)$  Distribution function which measure the number of carrier (k, r)

The distribution function can change through

(i) Diffusion Carriers of velocity  $v_k$  enter whilst others leave

$$\dot{f}_k \Big|_{diff} = -v_k \cdot \frac{\partial f_k}{\partial r}$$

(ii) External fields  $\dot{\mathbf{k}} = -\frac{e}{\hbar} (\mathbf{E} + \mathbf{v}_k \wedge \mathbf{H})$   $f_k \rightarrow f_{k+t\dot{\mathbf{k}}}$

$$\dot{f}_k \Big|_{field} = -\frac{e}{\hbar} (\mathbf{E} + \mathbf{v}_k \wedge \mathbf{H}) \cdot \frac{\partial f_k}{\partial \mathbf{k}}$$

(iii) Scattering Several processes throw carries from one state to another through interaction or collision

$$\dot{f}_k \Big|_{scatt}$$

# Reminders

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Total rate of change:  $\dot{f}_k = \dot{f}_k|_{diff} + \dot{f}_k|_{field} + \dot{f}_k|_{scatt}$

$$-\mathbf{v}_k \cdot \frac{\partial f_k}{\partial \mathbf{r}} - \frac{e}{\hbar} (\mathbf{E} + \mathbf{v}_k \wedge \mathbf{H}) \cdot \frac{\partial f_k}{\partial \mathbf{k}} = \dot{f}_k|_{scatt} \quad \text{and} \quad \mathbf{J} = \int e \mathbf{v}_k f_k d\mathbf{k}$$

**Boltzmann equation**

Rq: (i) Isotropic condition:  $\mathbf{J} = \frac{e^2 \tau}{4\pi^3 \hbar} \int \mathbf{v}_k d\mathbf{S} \cdot \mathbf{E}$

(ii) Shockley-Chambers tube integral

$$\sigma_{x\beta} = -\frac{e^3 B}{2\pi^2 \hbar^2} \int_0^T \left( \int_0^\infty v_x(t) e^{-t'/\tau(t)} v_\beta(t+t') dt' \right) dt$$



# Quantum oscillations

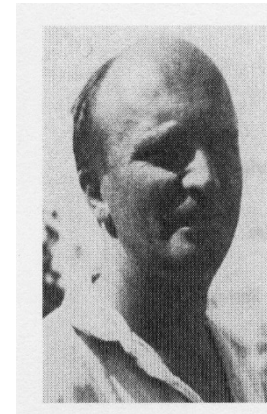
## 1930 de Haas-van Alphen / Shubnikov-de Haas effect



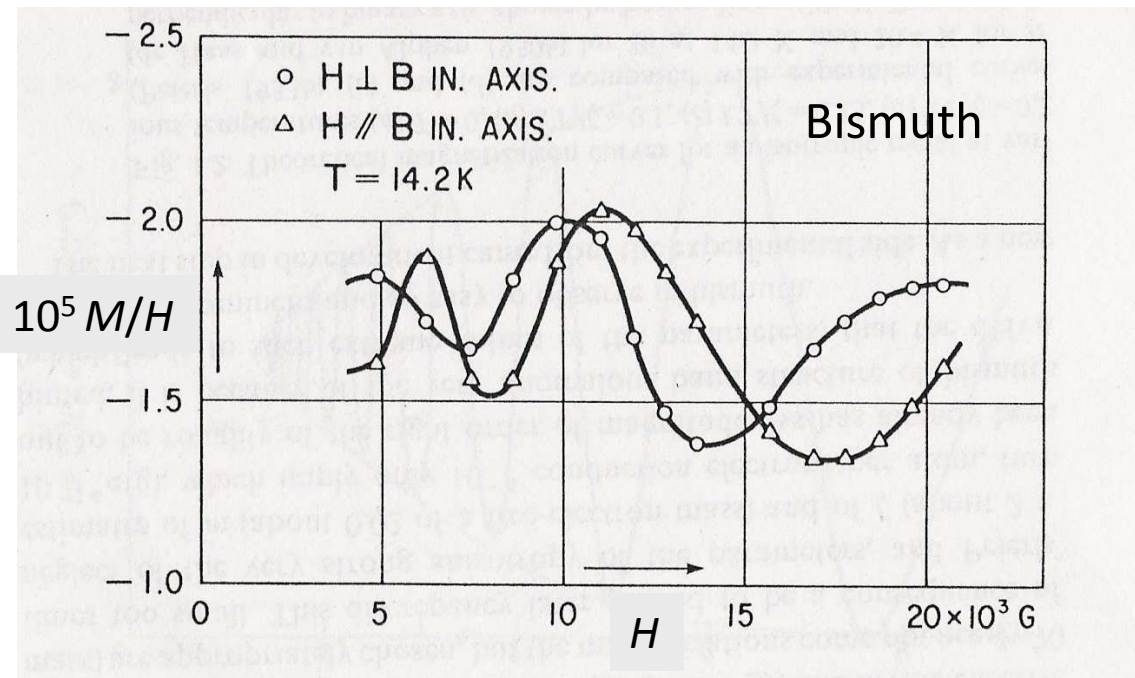
W.J. de Haas  
(1878-1960)



P.M. van Alphen  
(1906-1967)



L.V. Shubnikov  
(1901-1945)

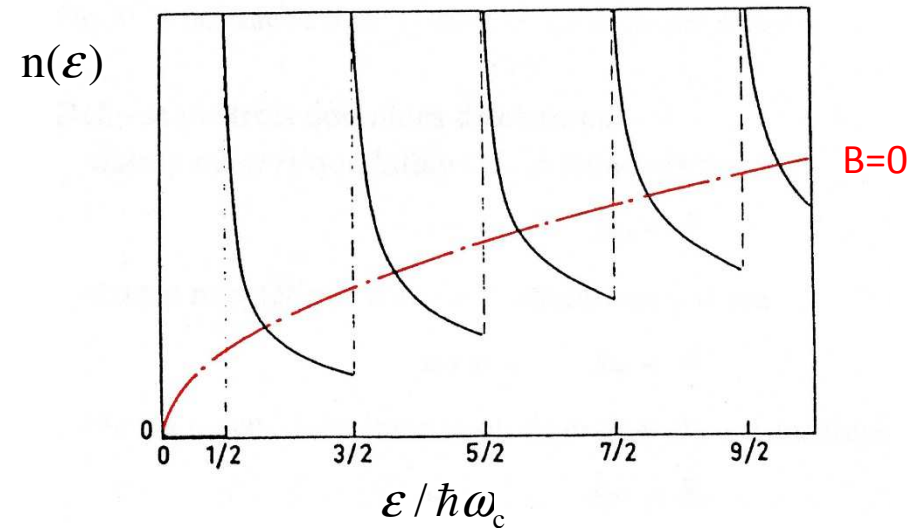
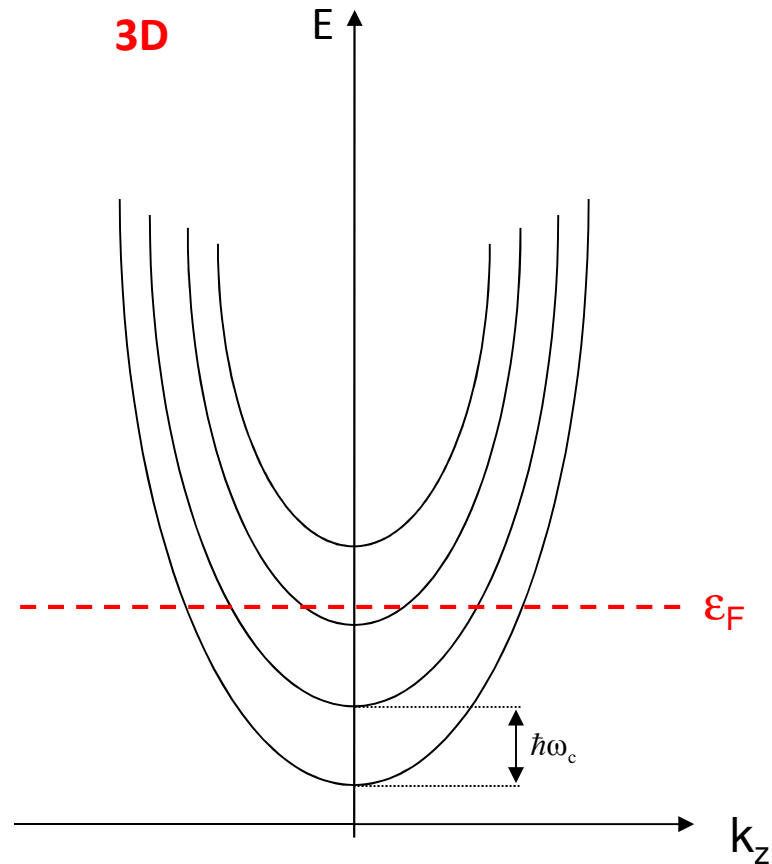


# Quantum oscillations

$$E = E_z + E_\perp = \frac{\hbar^2 k_z^2}{2m} + \hbar\omega_c \left( n + \frac{1}{2} \right) \quad \omega_c = \frac{qB}{m_c}$$

$$n(E) = 2\pi V \left( \frac{2m}{\hbar^2} \right)^{3/2} \hbar\omega_c \sum_{n=0}^{\infty} \frac{1}{\sqrt{E - \hbar\omega_c(n+0.5)}}$$

## Density of states



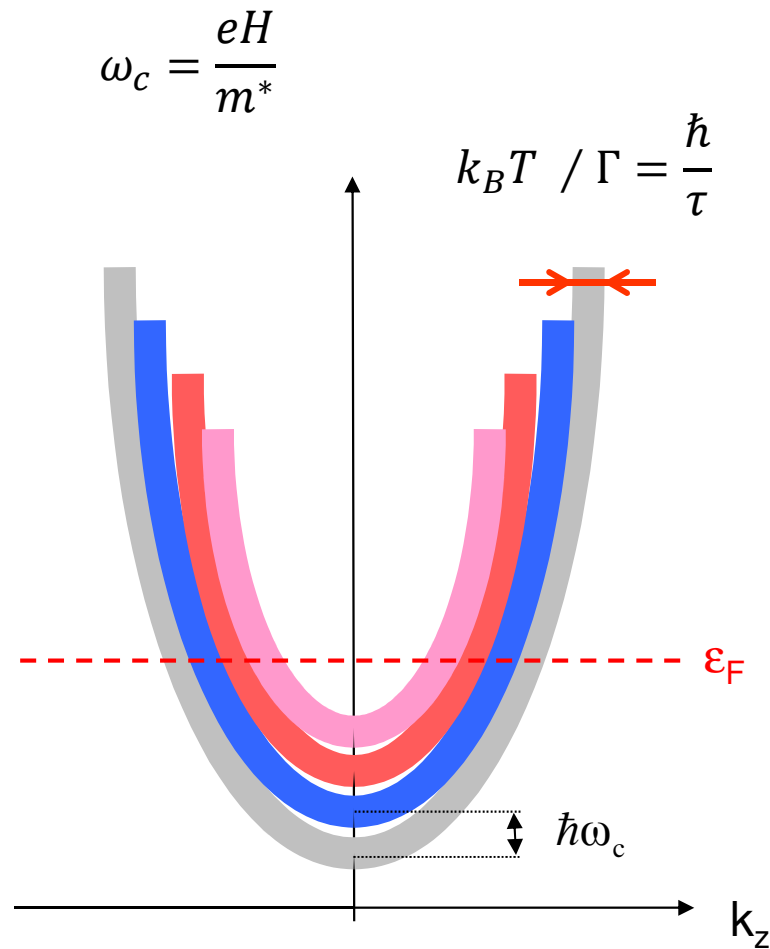
Oscillation of most electronic properties

Magnetization: de Haas-van Alphen (dHvA)

Resistivity: Shubnikov-de Haas (SdH)

# Quantum oscillations

Temperature / Disorder effects on quantum oscillations



- Low T measurements

$$\hbar\omega_c > k_B T$$

- Need high quality single crystals

$$\hbar\omega_c > \frac{\hbar}{\tau} \Rightarrow \omega_c \tau > 1$$

# Quantum oscillations

## Lifshitz-Kosevich theory (1956)

$T \neq 0$

$p=1$

$$\Delta R, \Delta M \propto R_T R_D R_S \sin \left[ 2\pi \left( \frac{F}{B} - \gamma \right) \right]$$

$$\frac{F}{B} = \frac{\hbar}{2\pi q} \frac{A_F}{B}$$

Onsager relation  $\Rightarrow$

$$A_F$$

Extremal area

$$R_T = \frac{X}{sh(X)} \quad \text{where } X = 14.694 \times T m_c / B$$

$$\Rightarrow m^*$$

Cyclotron mass

$$R_D = \exp\left(-\frac{14.694 \times T_D m_c}{B}\right) = \exp\left(-\frac{\pi}{\mu B}\right)$$

$$\Rightarrow T_D = \frac{\hbar}{2\pi k_B \tau}$$

Dingle temperature  
(mean free path)

$$R_S = \cos\left(\frac{\pi}{2} m_b^* g\right)$$

$$\Rightarrow m_b^* g$$

Direct measure of the Fermi surface extremal area

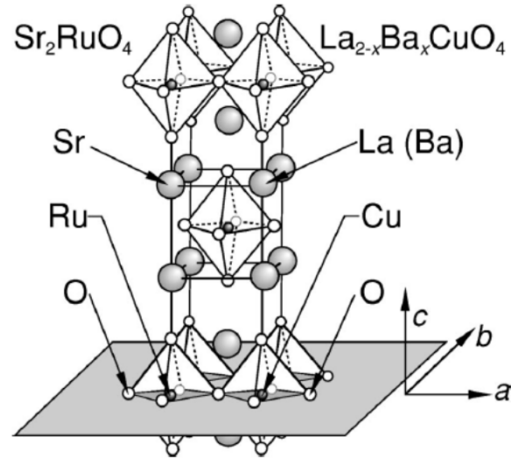
(but number of orbits ? location in k-space ?)

Rq: Luttinger theorem at 2D

$$n_{2D} = \frac{2A_k}{(2\pi)^2} = \frac{F}{\phi_0}$$

# Quantum oscillations: the case of $\text{Sr}_2\text{RuO}_4$

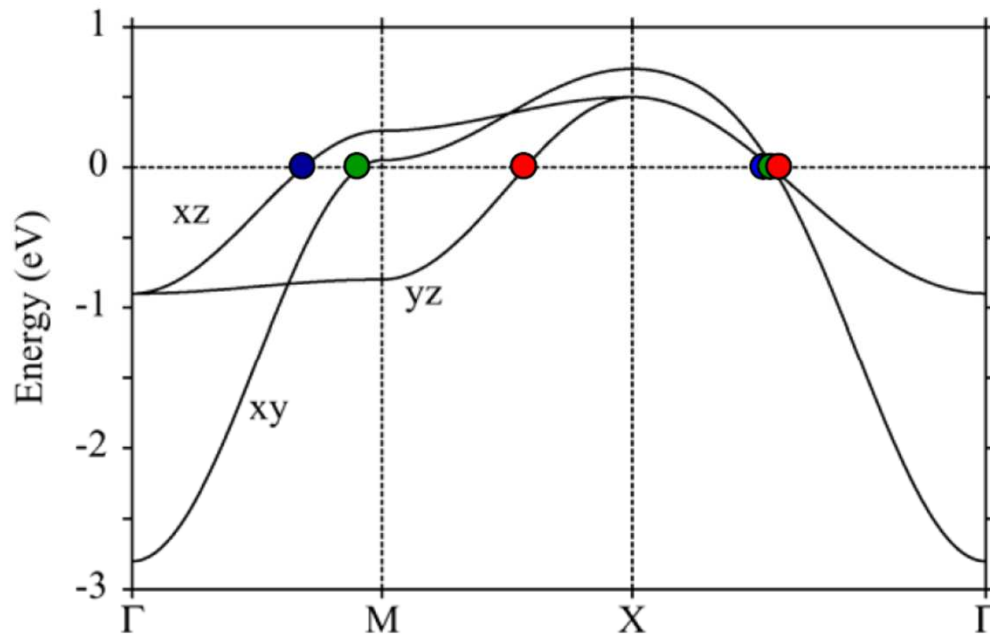
**$\text{Sr}_2\text{RuO}_4$ : a Quasi-2D Fermi liquid**



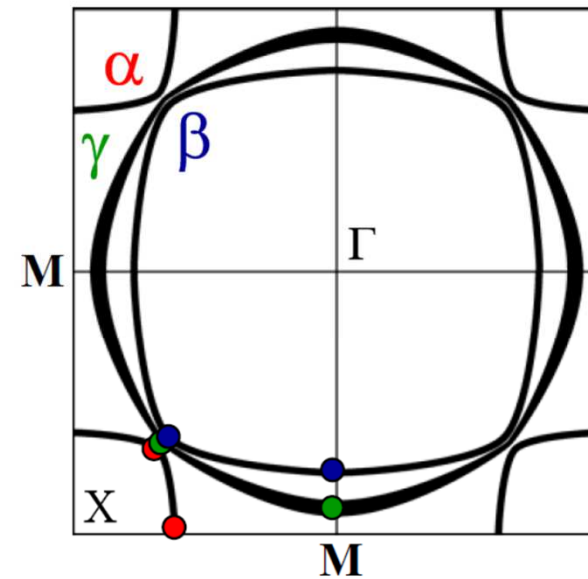
Band structure calculations

3 sheets of FS

$\alpha$  hole like  
 $\beta, \gamma$  electron like

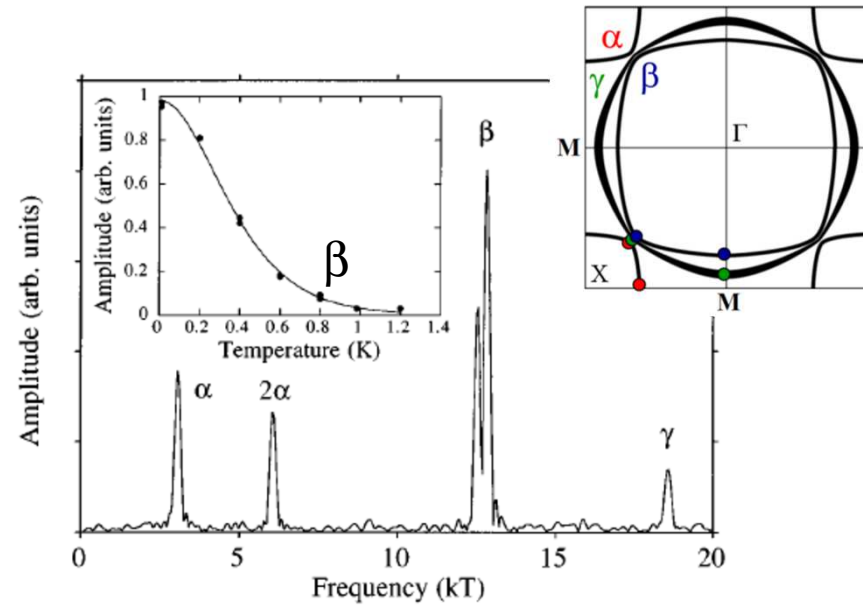
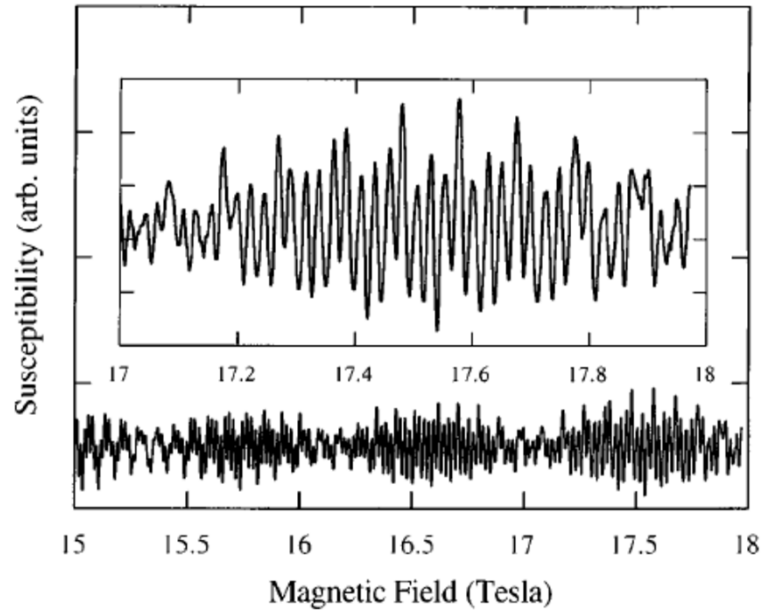


A. Liebsch *et al*, PRL **84**, 1591 (2000)



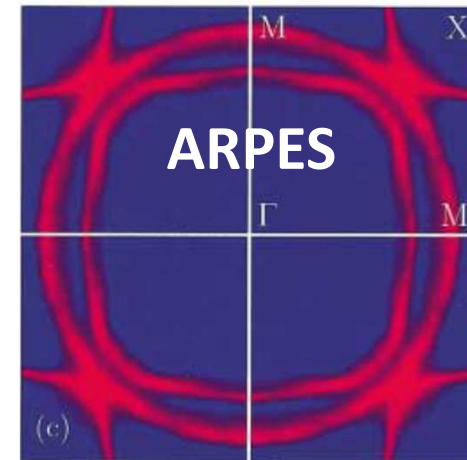
I.I. Mazin *et al*, PRL **79**, 733 (1997)

# Quantum oscillations: the case of $Sr_2RuO_4$



Mackenzie *et al*, *PRL* **76** 3786 (1996)

	$\alpha$	$\beta$	$\gamma$
Frequency $F$ (kT)	3.05	12.7	18.5
Average $k_F$ ( $\text{\AA}^{-1}$ )	0.302	0.621	0.750
$\Delta k_F/k_F$ (%)	0.21	1.3	<0.9
Cyclotron mass ( $m_e$ )	3.4	6.6	12.0
Band calc. $F$ (kT)	3.4	13.4	17.6
Band calc. $\Delta k_F/k_F$ (%)	1.3	1.1	0.34
Band mass ( $m_e$ )	1.1	2.0	2.9

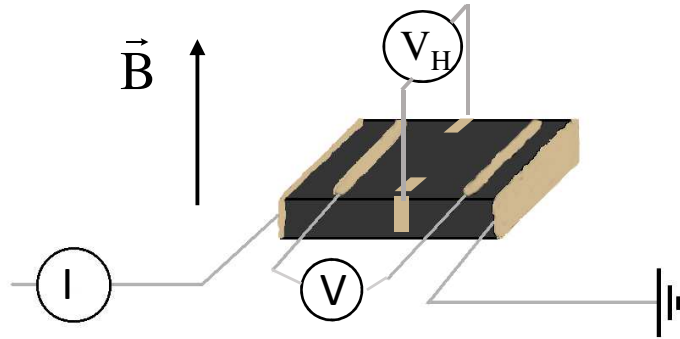


$Sr_2RuO_4$  cleaved at 180 K  
 $T = 10$  K  $h\nu = 28$  eV

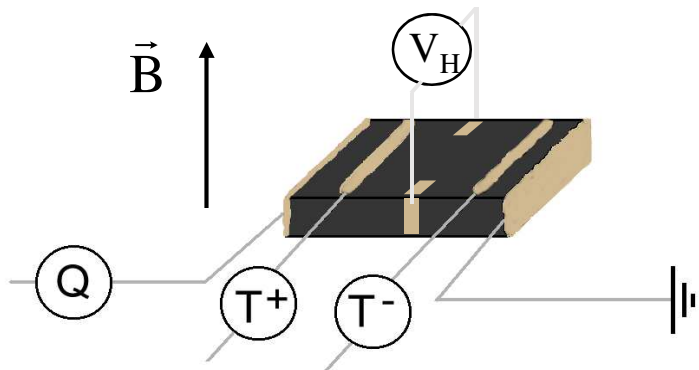
Damascelli *et al*, *PRL* **85** 5194 (2000)

## 2. *Experimental techniques*

# Electrical transport vs Thermal transport



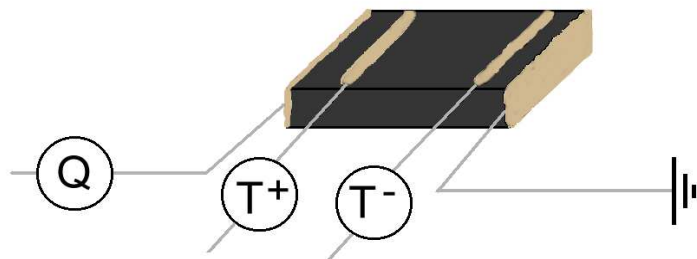
- Resistivity
- Hall effect



- Seebeck coefficient
- Nernst coefficient

$$S = \frac{\alpha}{\sigma T} = \frac{E_x}{\nabla_x T}$$

$$v = \frac{N}{B} = \frac{1}{B_z} \frac{E_y}{\nabla_x T}$$

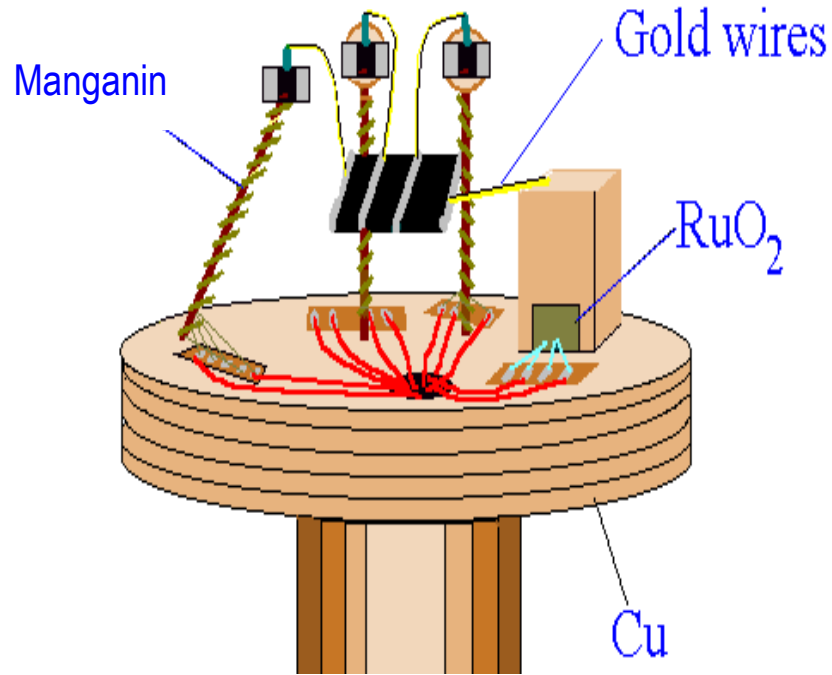


- Thermal conductivity

$$\kappa(T) = \frac{Q}{\Delta T}$$



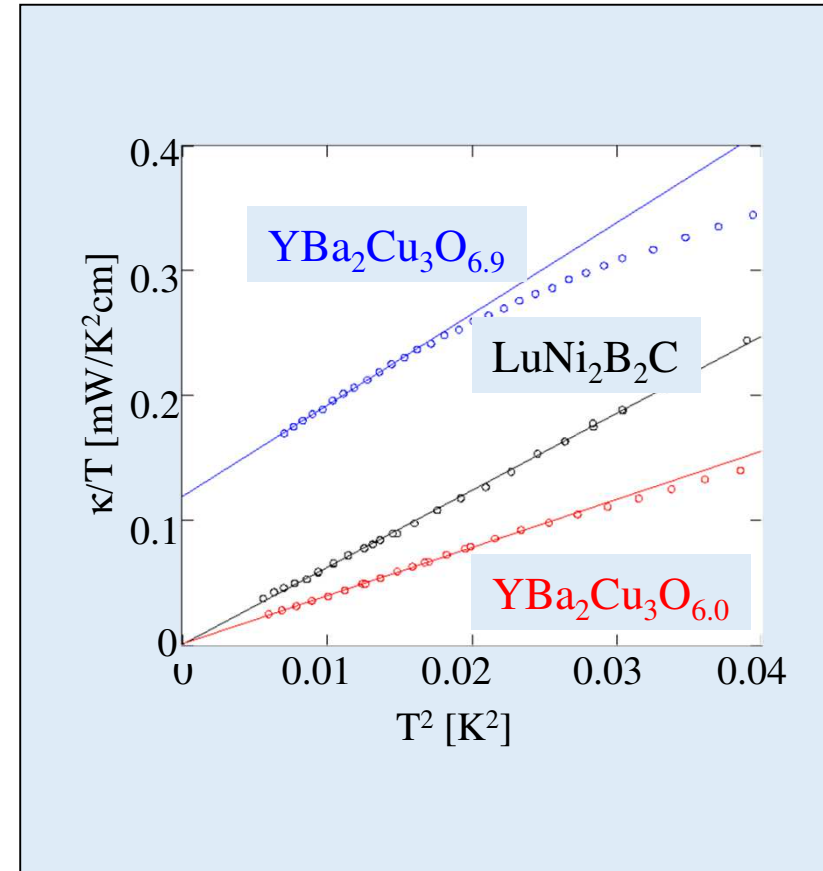
# Thermal transport setup



Courtesy of K .Behnia

Subkelvin temperature measurement:

$$\kappa(T) = \kappa_{\text{phonon}}(T) + \kappa_{\text{electronic}}(T)$$



insulator:  $a = 0$

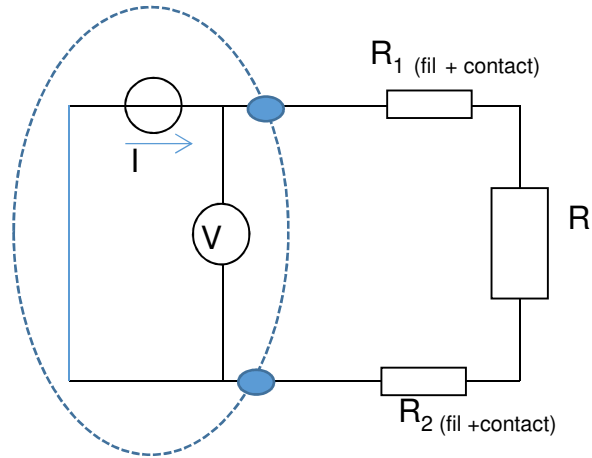
*s*-wave superconductor:  $a = 0$

*d*-wave superconductor :  $a \neq 0$

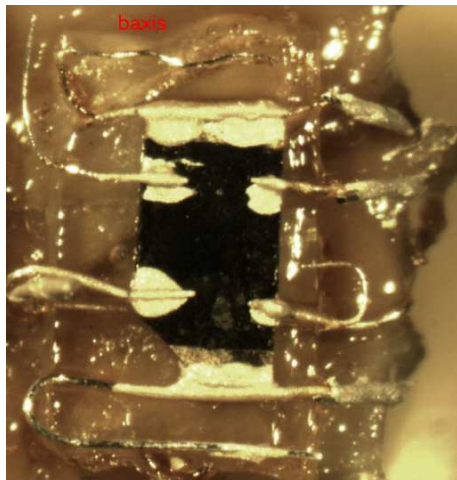
YBCO (optimal)

# Electrical transport measurements

## 2 points measurements

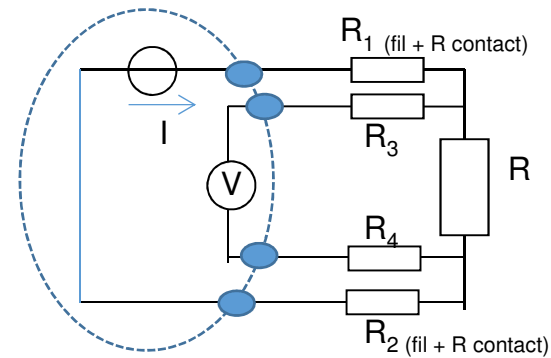


Sample connected with silver paint



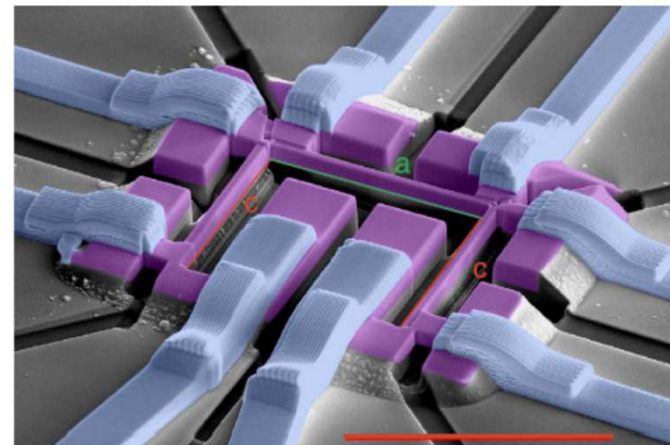
$\sim 400 \mu\text{m}$

## 4 points measurements



Microstructures (FIB carved) of  $\text{CeRhIn}_5$

$\sim 60 \times 60 \mu\text{m}$

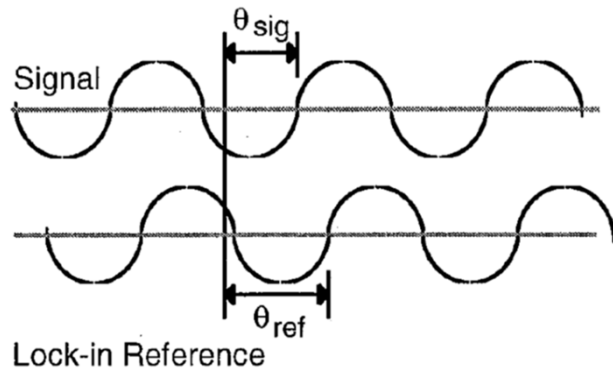


Moll et al, *Nature Comm.* **6**, 6663 (2015)

# Lock-in amplifier

## Phase-sensitive detection

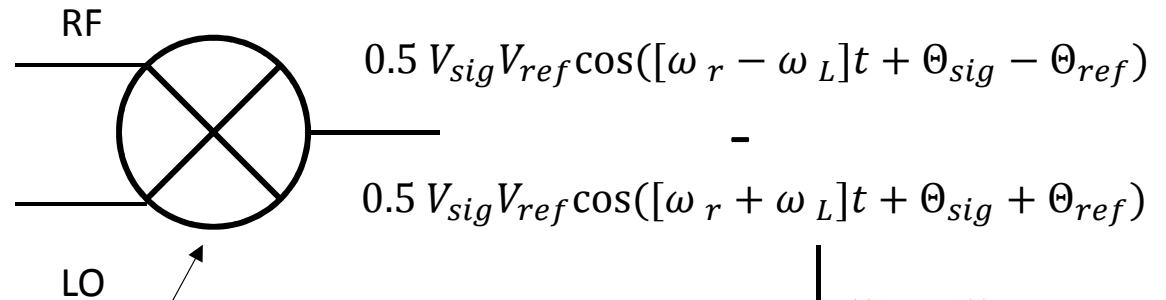
$$V_{sig} = V_{sig} \sin(\omega_r t + \Theta_{sig})$$



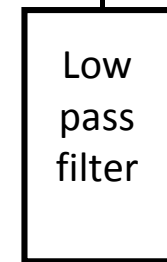
$$V_{ref} = V_L \sin(\omega_L t + \Theta_{ref})$$

Output of a mixer (PSD) = product of two sine waves

This technique allows to detect the response from the experiment at the reference frequency (narrow band detection much better than a simple filter)



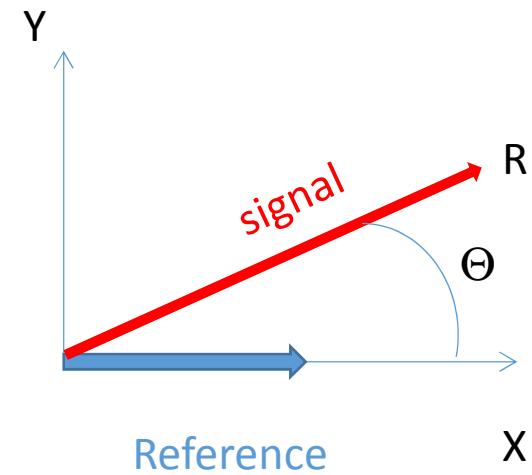
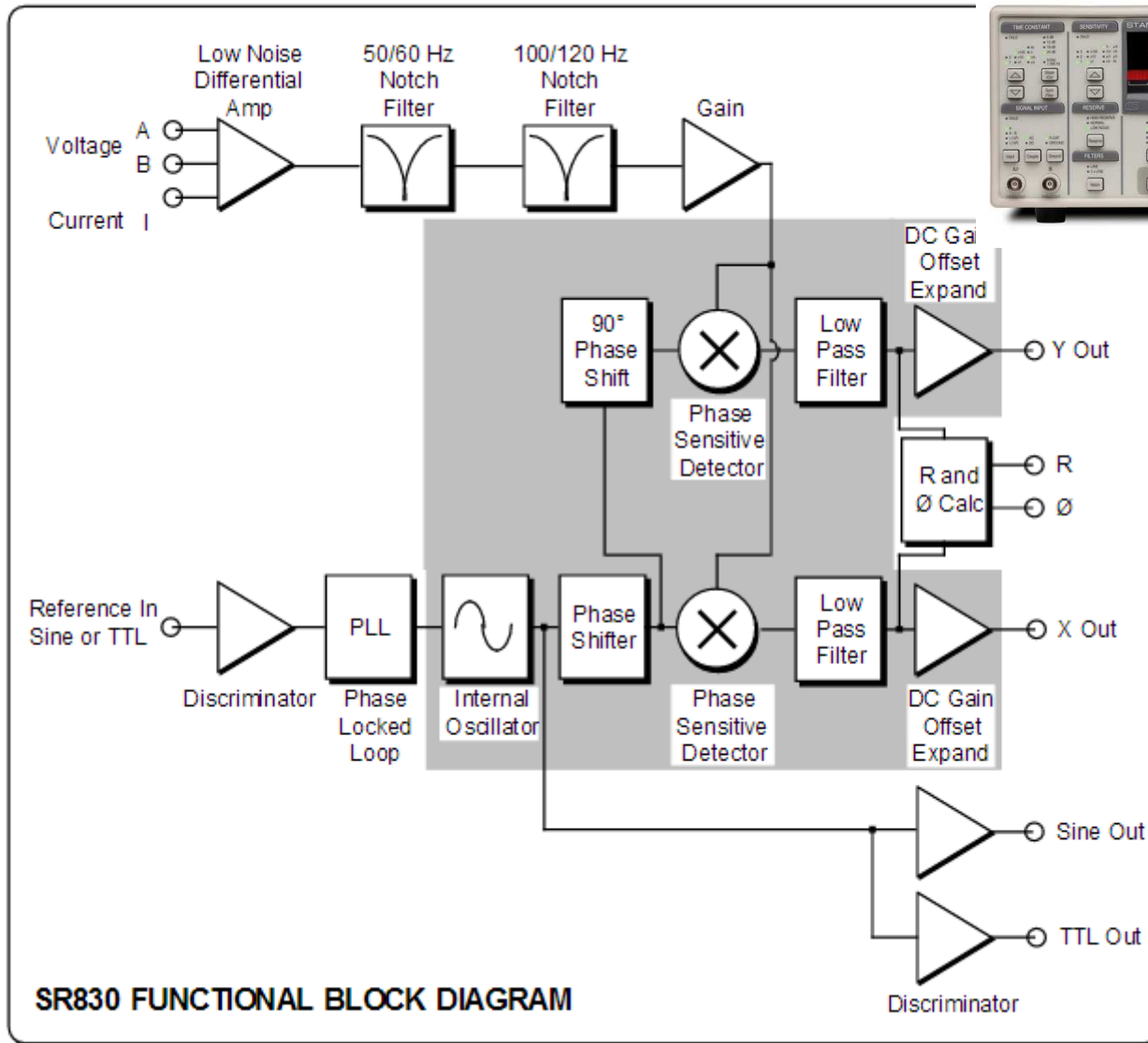
$$\omega_r = \omega_L$$



$$0.5 V_{sig} V_{ref} \cos(\Theta_{sig} - \Theta_{ref})$$

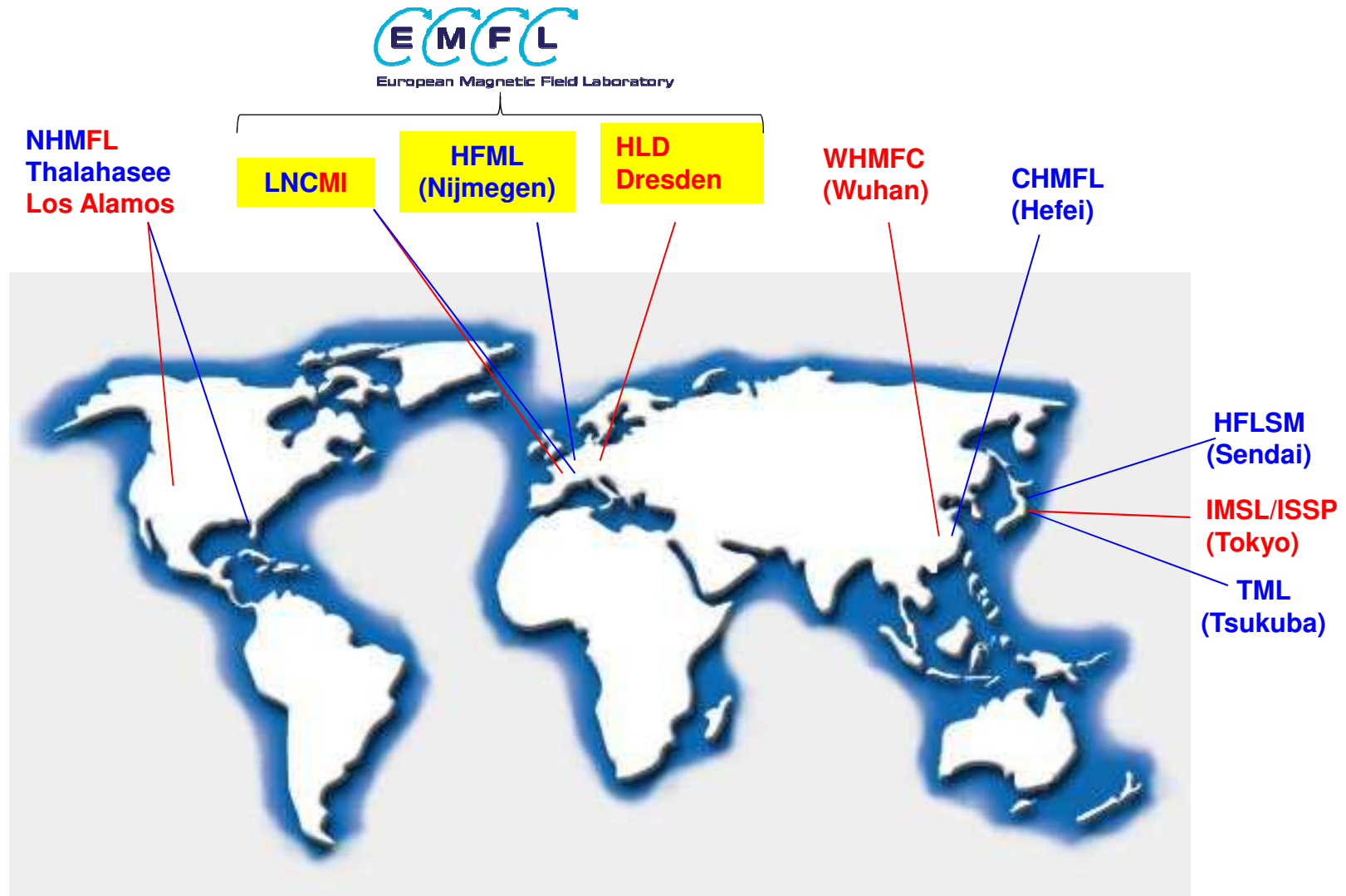
DC signal if  $\Theta_{sig} - \Theta_{ref} = c^{te}$

# Lock-in amplifier



# High magnetic field facility

Large high magnetic field facilities (**pulsed** and **DC**)





# LNCMI-Grenoble: static fields

Resistive coil

$I_{\max} = 32\,000\text{ A}$ ,  $P = 24\text{ MW}$

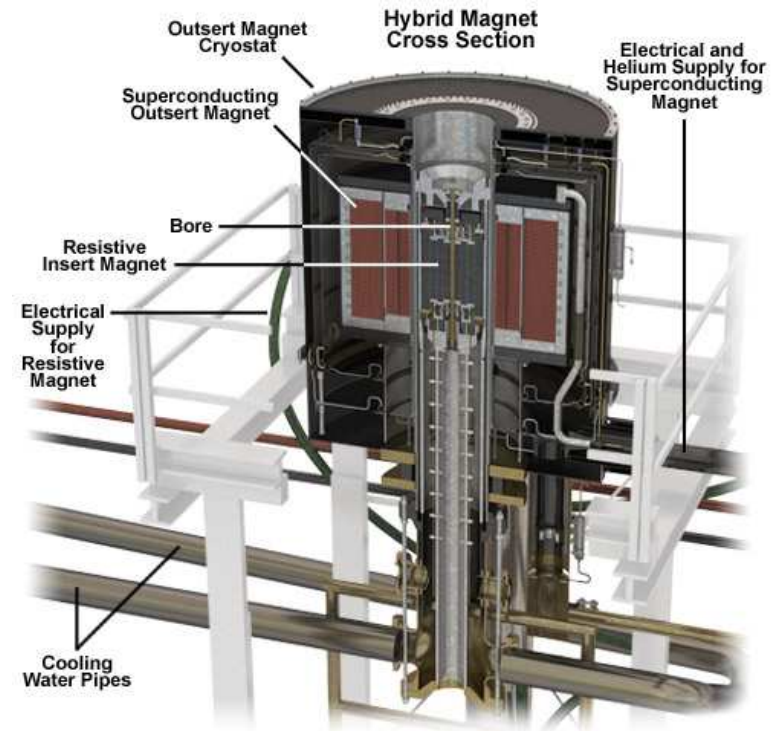
Water flow  $\sim 300\text{ L/s}$  (for cooling)

Max. field = 36.5 T



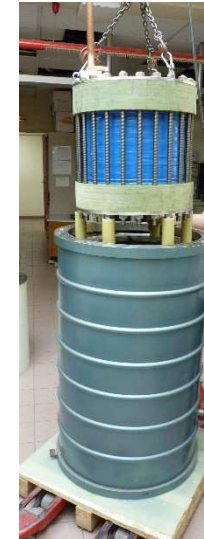
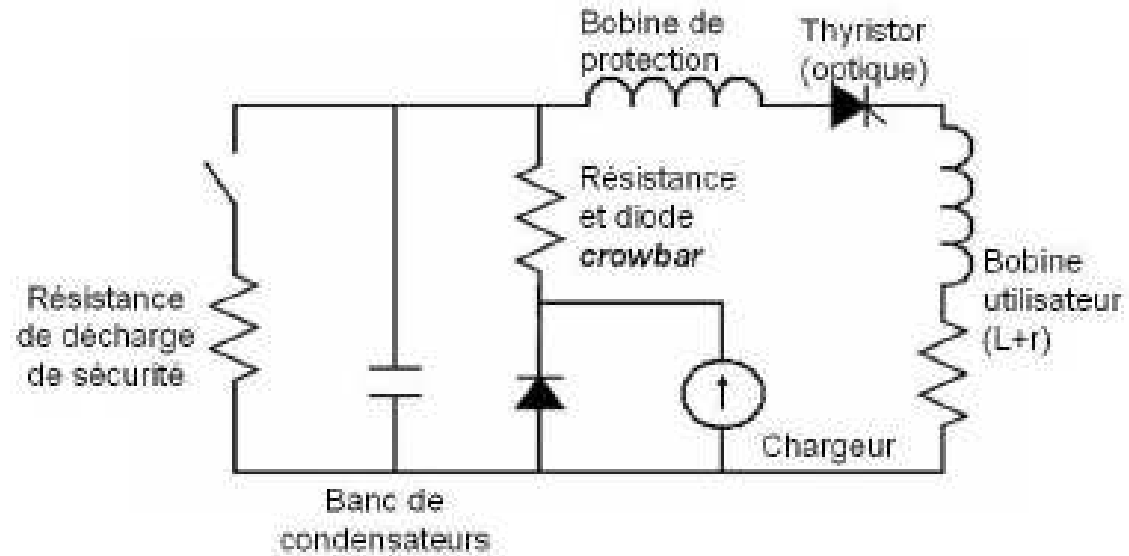
Hybrid project (2019)

34 T (R) + 9 T (SC) = 43 T



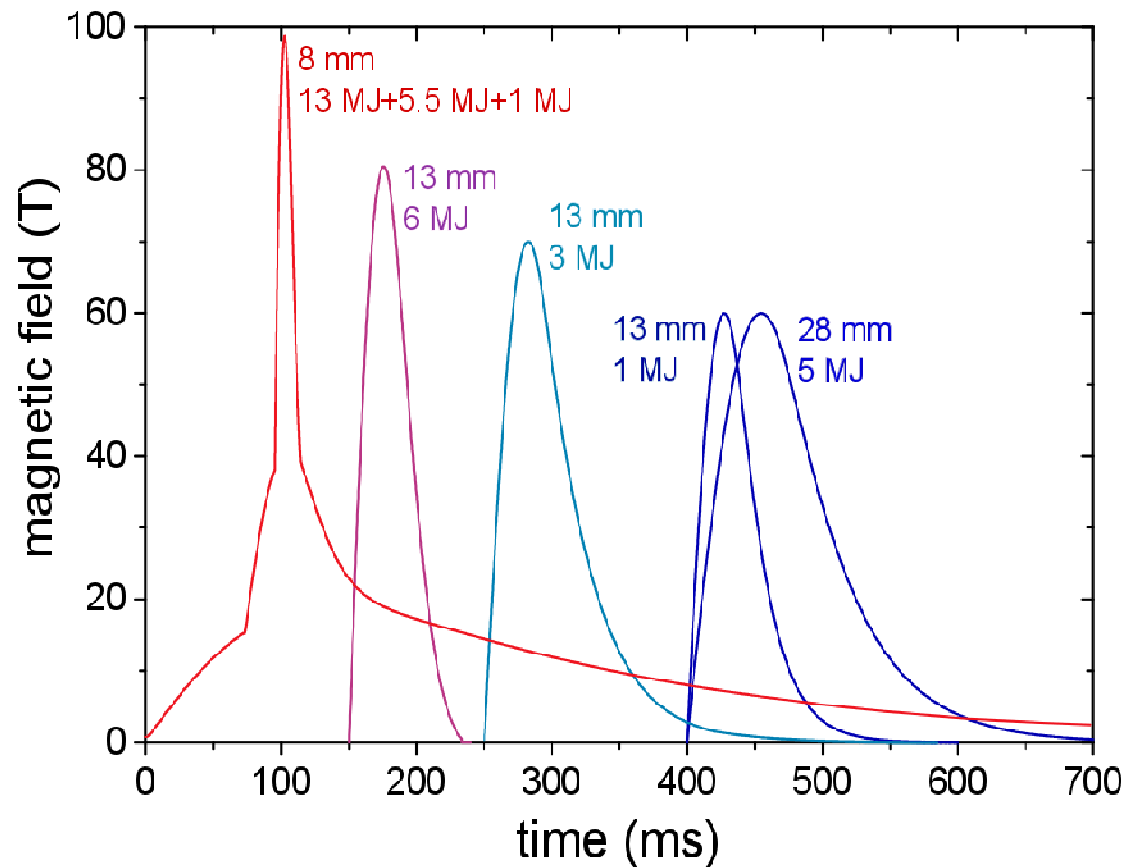
NHMFL Tallahassee (45 T)

# LNCMI-Toulouse: pulsed fields

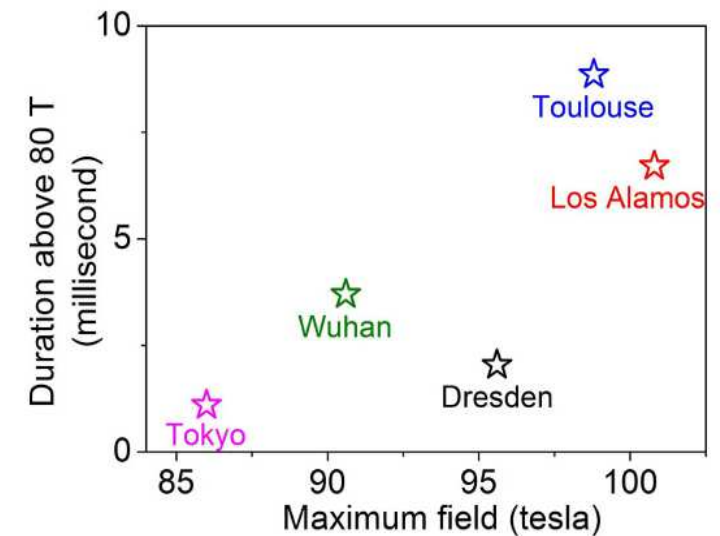


# LNCMI-Toulouse: pulsed fields

## High magnetic fields up 98.8 T



100 T coil





### 3. *Transport properties of SCES*

Inspired by a talk of N. Hussey

# Transport properties of SCES

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**What makes DC transport measurements such an important probe of SCES ?**

✓ “ Often the first thing to be measured, but the last to be understood...”

✓ “ What scatters may also pair ”

Hence electrical resistivity is a powerful, albeit coarse, probe of superconductivity

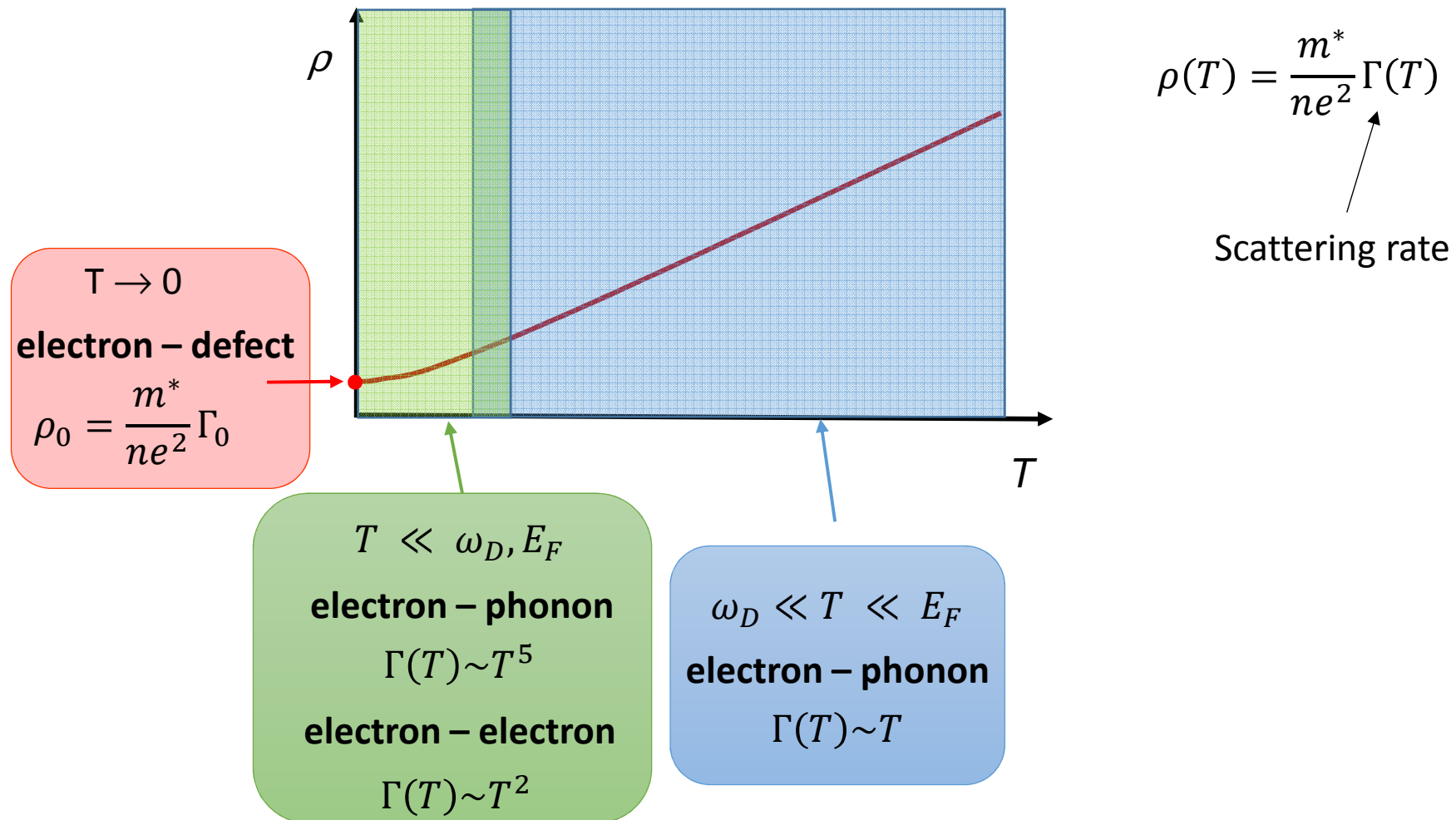
✓ In the Fermi liquid picture the resistivity is  $T^2$  with  $A / \gamma^2 \approx 10^{-5} \mu\Omega \text{ cm mol}^2 \text{ K}^2/\text{J}^2$

✓ Close to a quantum critical point the resistivity is linear in  $T$

*High temperature: bad metals*

# What constitutes metallic behaviour?

**Basic definition:** A material whose resistivity increases with temperature



+ electron - any excitation (magnons...)

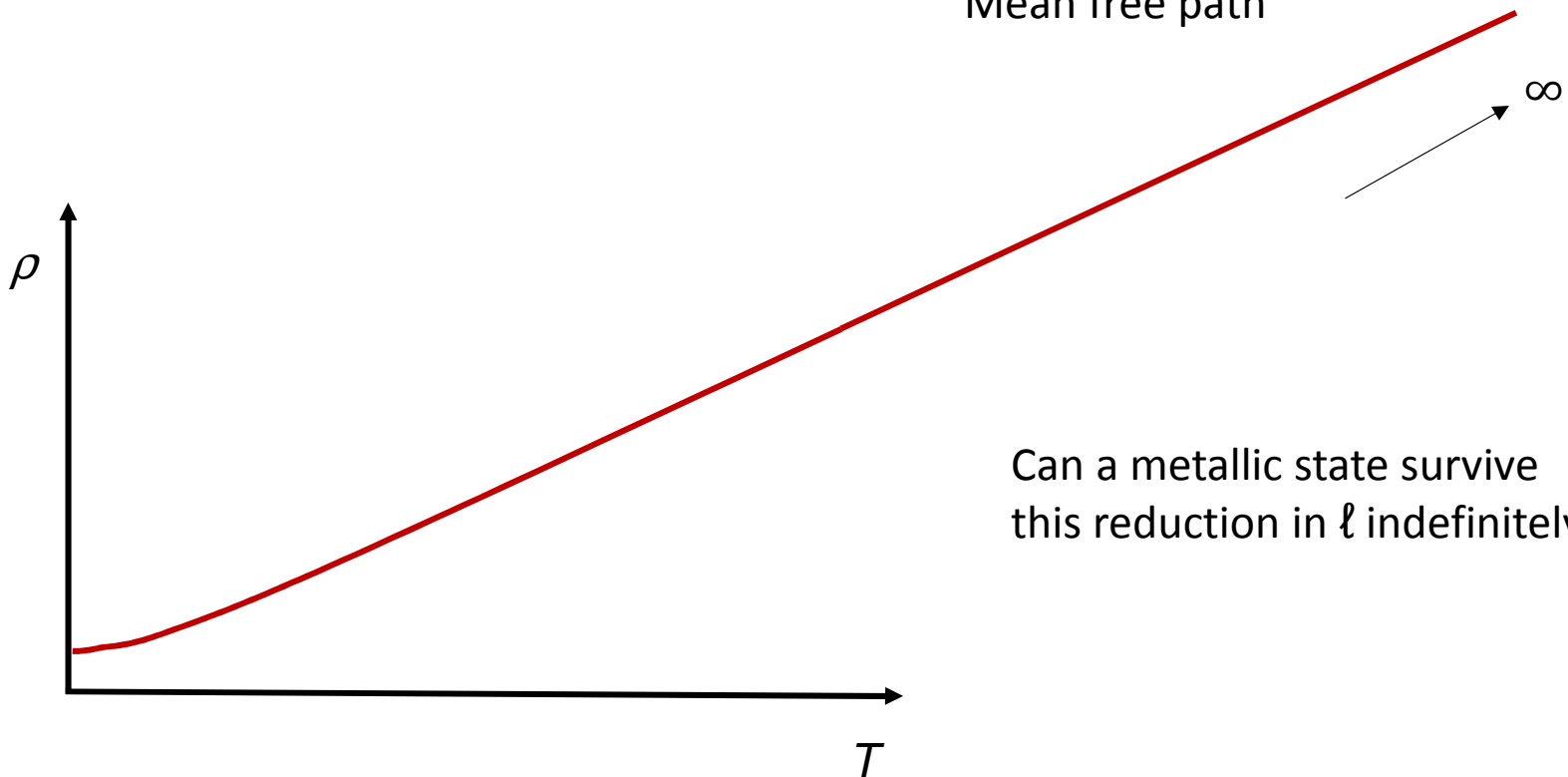
# What constitutes metallic behaviour?

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**Basic definition:** A material whose resistivity increases with temperature

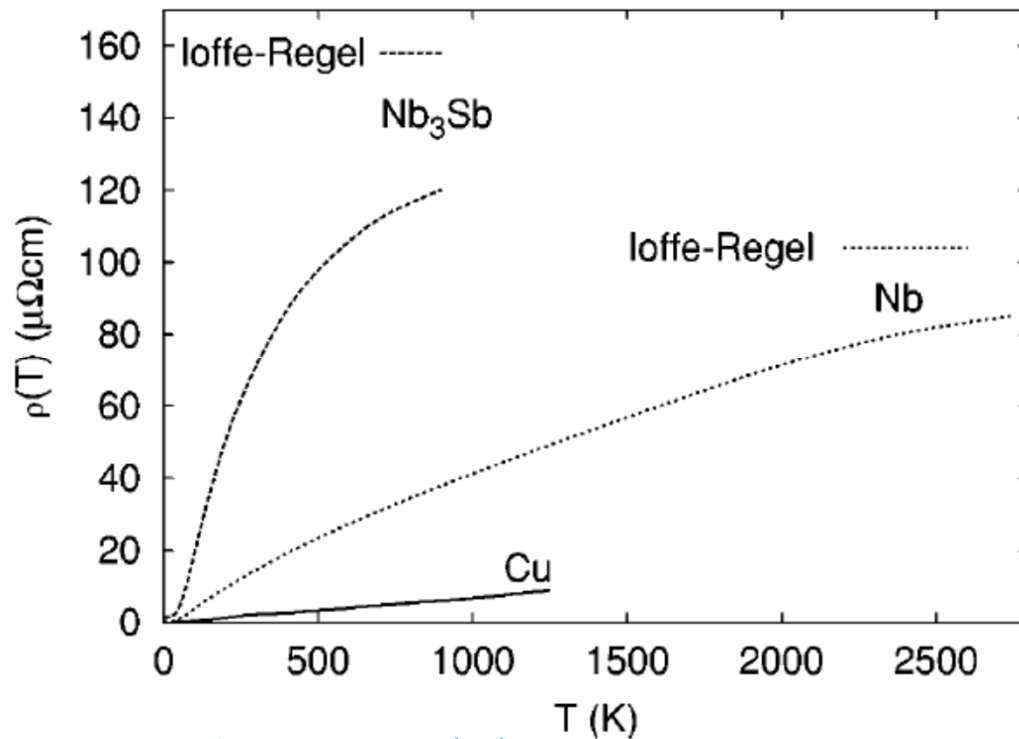
According to the Drude model:  $\rho(T) = \frac{m^*}{ne^2} \Gamma(T) \propto \frac{1}{\ell(T)}$

Mean free path



Can a metallic state survive this reduction in  $\ell$  indefinitely?

# Ioffe-Mott-Regel limit



Gunnarson *et al*, *RMP* **75** 1085 (03)

$$\rho(T) = \frac{m^*}{ne^2} \Gamma(T) \propto \frac{1}{\ell(T)}$$

Semiclassical theory breaks down if  $\ell$  become shorter than the interatomic distance  $a$

OR

$$\ell > \lambda_F = \frac{2\pi}{k_F}$$

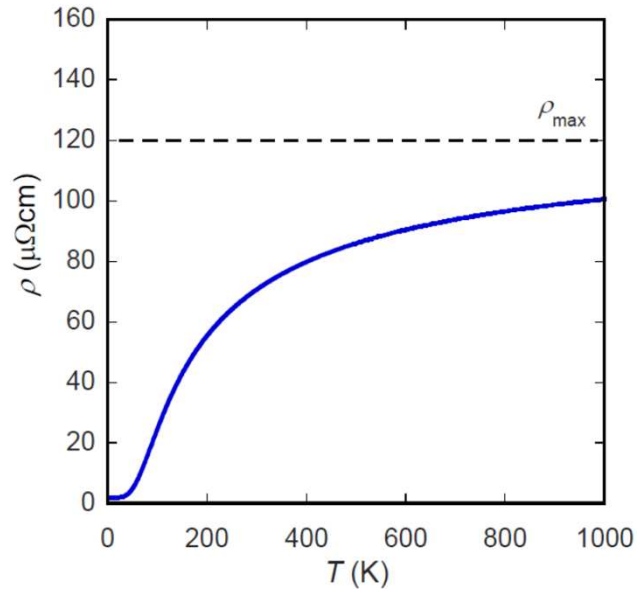
$$k_F \ell > 1$$

$\ell \approx a \Rightarrow$  saturation of the resistivity ( $\Delta k \sim$  size of Brillouin zone)

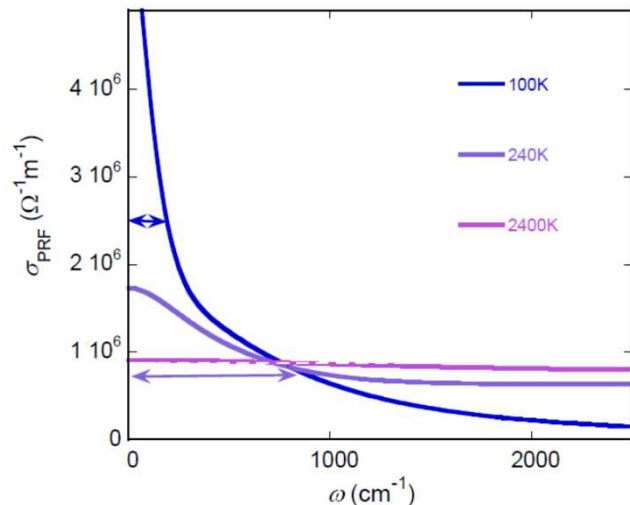
# Conventional metallic transport at high $T$

## Saturating metals

Hussey et al, *Phil. Mag* **84** 2847 (2004)



$$\sigma(\omega) = \frac{\sigma_0}{1 + \omega^2 \tau^2}$$

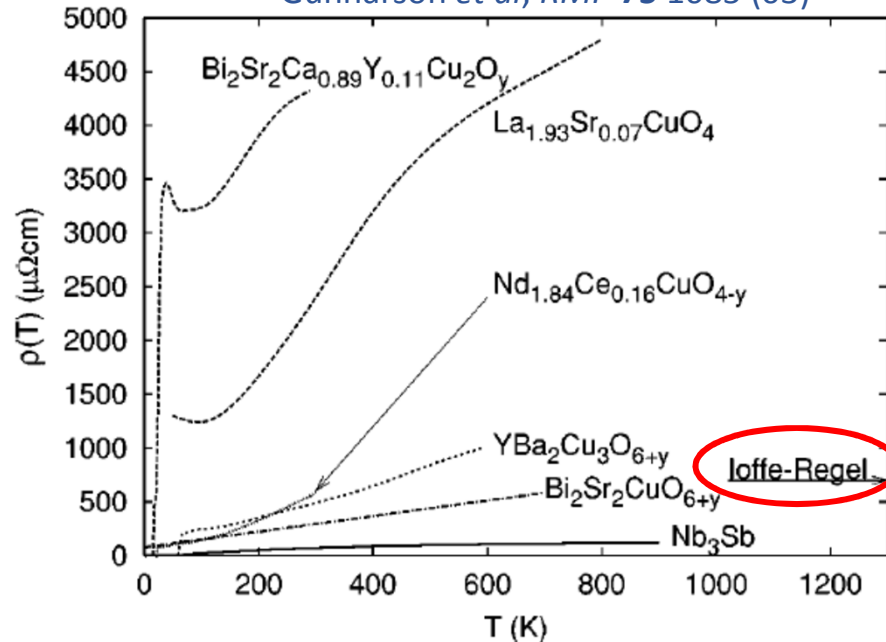


- Drude term = coherent QP contribution
- Peak centred at  $\omega = 0$  but extends up to  $W$
- Drude peak broadens at high  $T$  with a width at half-maximum equal to  $\Gamma(T < T_m)$
- Saturation of  $\rho \Leftrightarrow$  Loss of coherence of the QP  
 $\sigma(\omega, T)$  evolves into a plateau ( $T < W$ )

Spectral weight preserved below  $\omega \sim W$  (bandwidth)

# Bad metallic transport in cuprates

Gunnarson *et al*, *RMP* **75** 1085 (03)



Non saturating metals:  
High  $T_c$  cuprates, manganites, vanadates,  
ruthenates and organics

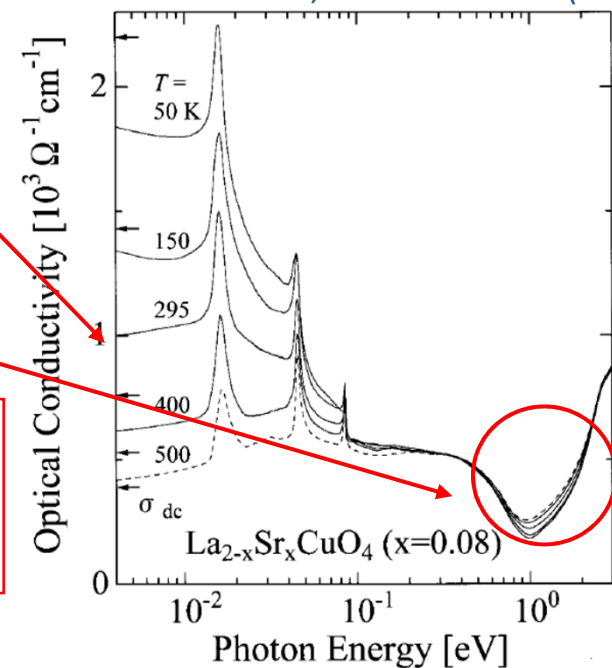
Universal feature of bad metals:

- Proximity to Mott insulator
- Strong e-e interaction

- Drude peak disappears around  $\sigma_0 \sim 700 - 1000 \Omega^{-1}\text{cm}^{-1}$  (value close to the MIR limit)
- Lost spectral weight recovered at  $\omega > W$

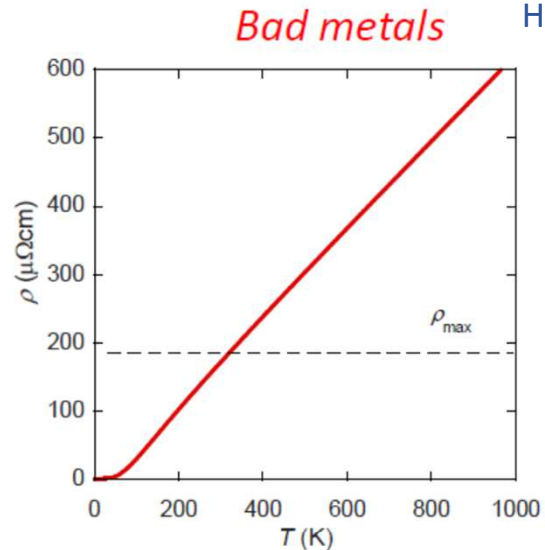
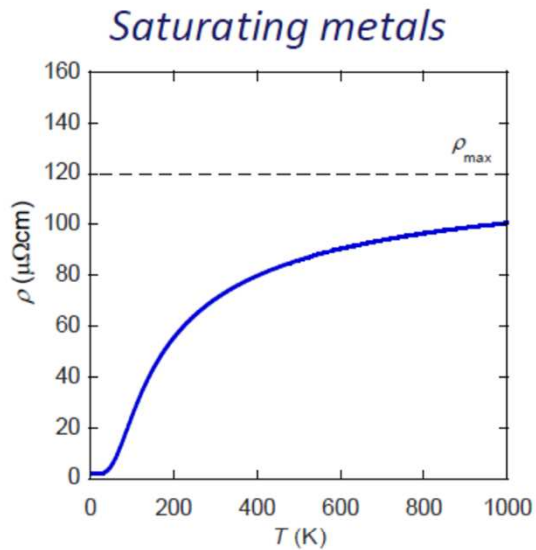
Coherent to incoherent cross-over in the optical conductivity along with the loss of spectral weight (within  $W$ ) may explain the non saturating resistivity in 'bad metals'

Takenaka *et al*, *PRB* **65** 092405 (02)

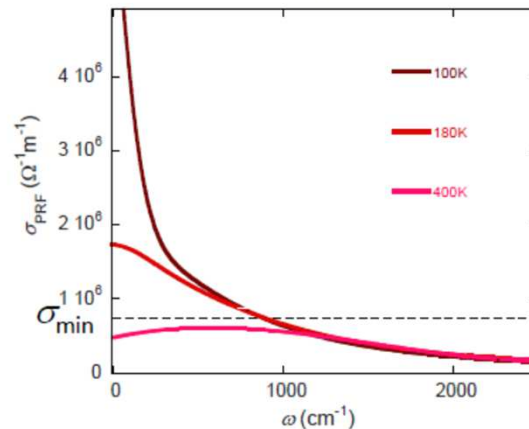
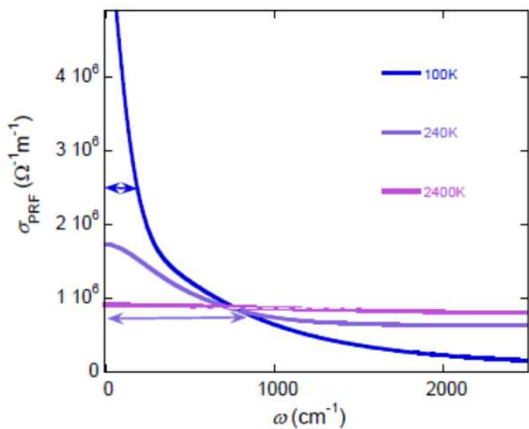




# Conventional vs bad metallic transport at high $T$



Hussey et al, *Phil. Mag* **84** 2847 (2004)



- ✓ Low  $\omega$  dip
- ✓ T-indept  $\sigma(\omega)$  at high  $\omega$
- ✓  $T_{\text{crit}}$  and  $\sigma_{\text{crit}}(0)$

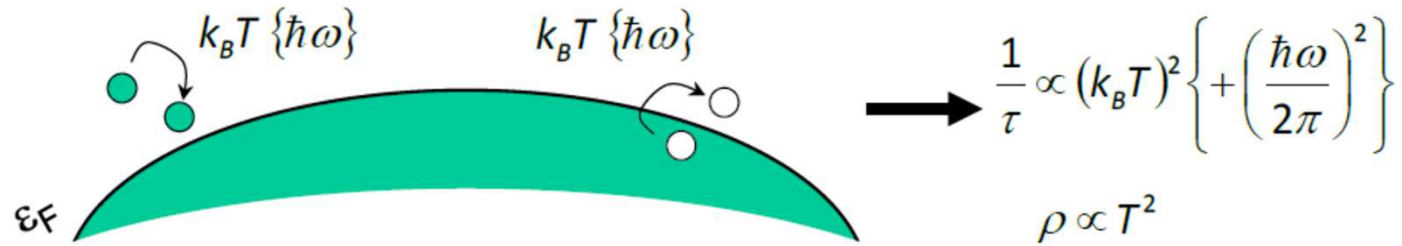
Spectral weight preserved below  $\omega \sim W$

Low-freq. spectral weight displaced to  $\omega > W$

A bad metal behaves as if it is a QP insulator which is rendered metallic by collective fluctuations (e.g. CDW, SDW, stripes...)

*Low temperature:  $T^2$  resistivity*

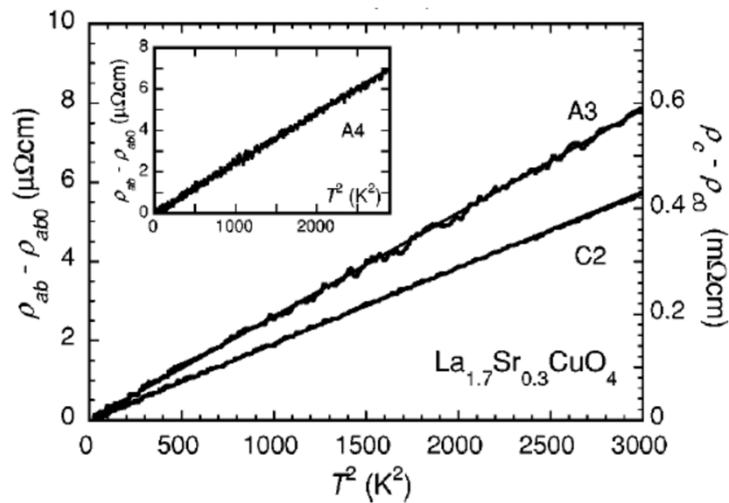
# Correlated Fermi liquid at low $T$



$T^2$  resistivity originates from electron-electron scattering processes near  $E_F$

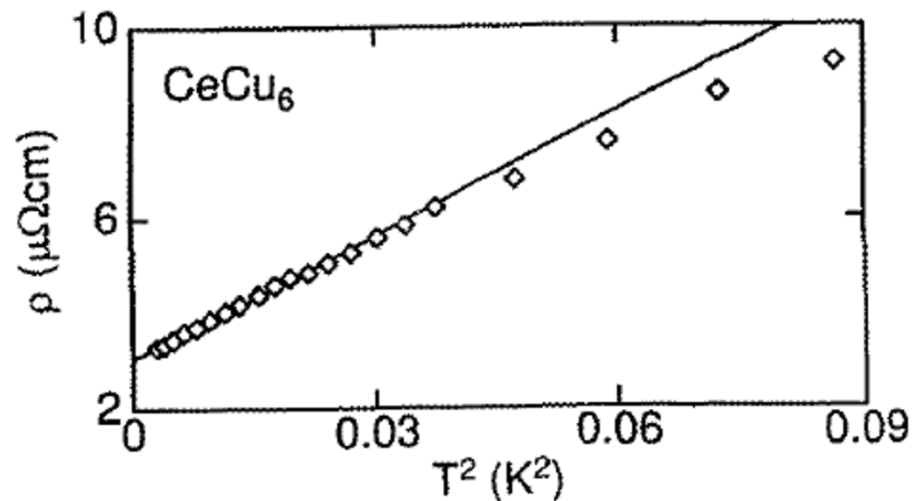
Electrons participating in the scattering event are those confined to a width of  $k_B T / E_F$

*Overdoped cuprates*



Nakamae *et al*, *PRB* **68** 100502 (2003)

*Heavy fermions*



Lohneysen, *JPCM* **8** 9689 (1996)

# Kadowaki-Woods ratio

$$\rho(T) = \rho_0 + AT^2$$

$$C_{el} = \gamma T = \frac{\pi^2}{6} k_B^2 N(\epsilon_F) T$$

$$A/\gamma^2 = \text{const.} \Rightarrow A \propto N(\epsilon_F)^2$$

Yamada & Yoshida, *Prog.Theor.Phys.* 76 621 (86)

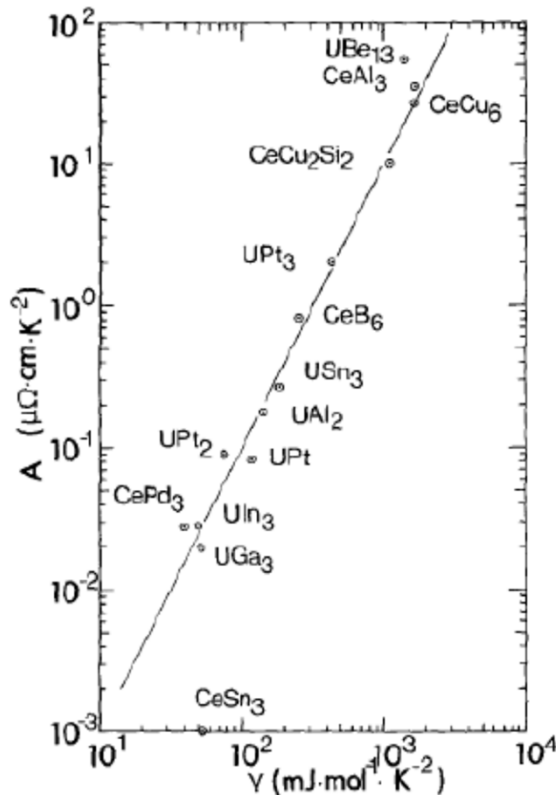
Auerbach & Levin, *JAP* 61 3162 (87)

Coleman, *PRL* 59 1026 (87)

Miyake, Matsuura & Varma, *SSC* 71 1149 (89)

Kontani, *JPSJ* 73 515 (04)

⋮



Kadowaki & Woods,  
*SSC* 58 507 (86)

$$A/\gamma^2 \sim a_0 = 10^{-5} \mu\Omega\text{cm}\cdot\text{mol}^2\cdot\text{K}^2/\text{J}^2$$

$$A \propto \gamma_0^2 \propto m^{*2}$$

$$A_i = \left( \frac{8\pi^3 a c k_B^2}{e^2 \hbar^3} \right) \cdot \left( \frac{m_i^{*2}}{k_{Fi}^3} \right)$$

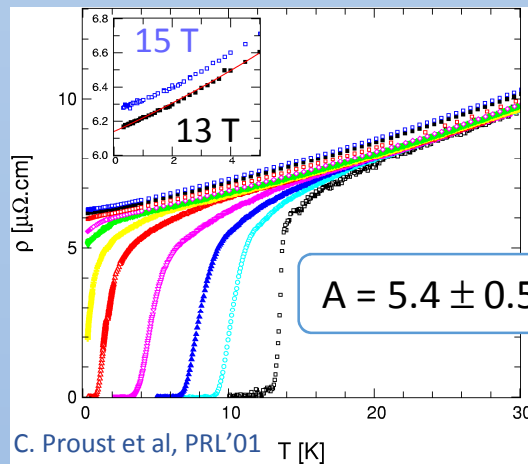
Hussey, *JPSJ* 74 1107 (2005)

# Correlated Fermi liquid at low $T$

$$\rho = \rho_0 + A T^2$$

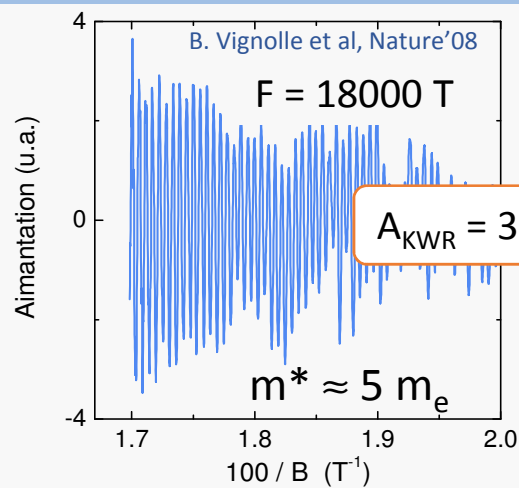
$$A_i = \left( \frac{8\pi^3 a c k_B^2}{e^2 \hbar^3} \right) \cdot \left( \frac{m_i^*}{k_{Fi}^3} \right)$$

$\text{Ti}_2\text{Ba}_2\text{CuO}_{6+\delta}$



$$A = 5.4 \pm 0.5 \text{ n}\Omega \text{ cm K}^{-2}$$

C. Proust et al, PRL'01

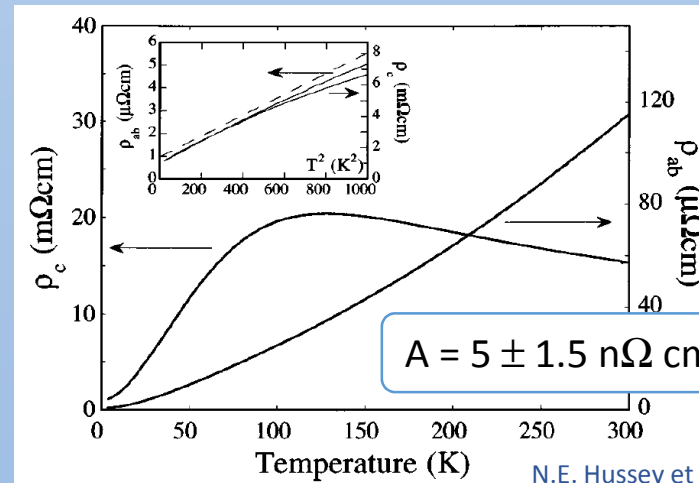


$$A_{\text{KWR}} = 3.9 \text{ n}\Omega \text{ cm K}^{-2}$$

$$m^* \approx 5 m_e$$

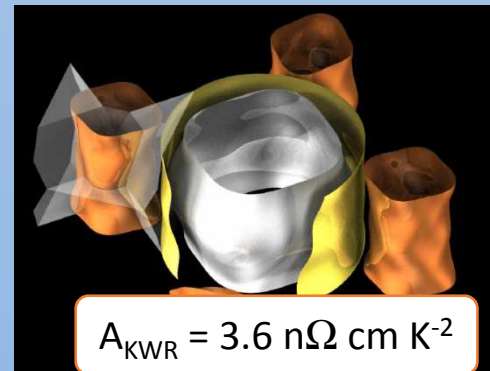
$\text{Sr}_2\text{RuO}_4$

Multi-band system  $\Rightarrow \frac{1}{A} = \sum_i \frac{1}{A_i}$



$$A = 5 \pm 1.5 \text{ n}\Omega \text{ cm K}^{-2}$$

N.E. Hussey et al, PRB'98



$$A_{\text{KWR}} = 3.6 \text{ n}\Omega \text{ cm K}^{-2}$$

TABLE II. Summary of quasiparticle parameters of  $\text{Sr}_2\text{RuO}_4$ .

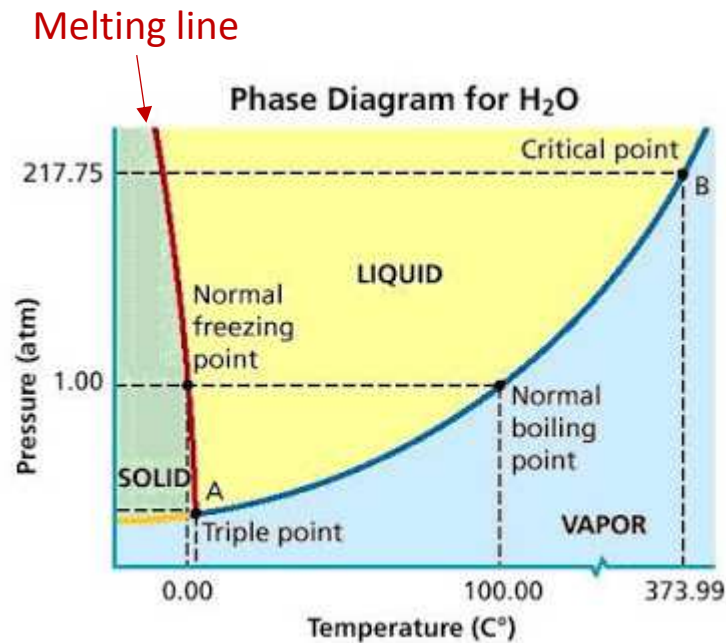
Fermi-surface sheet	$\alpha$	$\beta$	$\gamma$
Character	Holelike	Electronlike	Electronlike
$k_F$ ( $\text{\AA}^{-1}$ ) <sup>a</sup>	0.304	0.622	0.753
$m^*$ ( $m_e$ ) <sup>b</sup>	3.3	7.0	16.0
$m^*/m_{\text{band}}$ <sup>c</sup>	3.0	3.5	5.5
$v_F$ ( $\text{ms}^{-1}$ ) <sup>d</sup>	$1.0 \times 10^5$	$1.0 \times 10^5$	$5.5 \times 10^4$
$\langle v_F^2 \rangle$ ( $\text{m}^2 \text{s}^{-2}$ ) <sup>e</sup>	$7.4 \times 10^5$	$3.1 \times 10^6$	$1.0 \times 10^5$
$t_i$ (K) <sup>f</sup>	7.3	15.0	2.7

C. Bergemann et al, Ad. Phys.'03

*Low temperature: Quantum criticality*

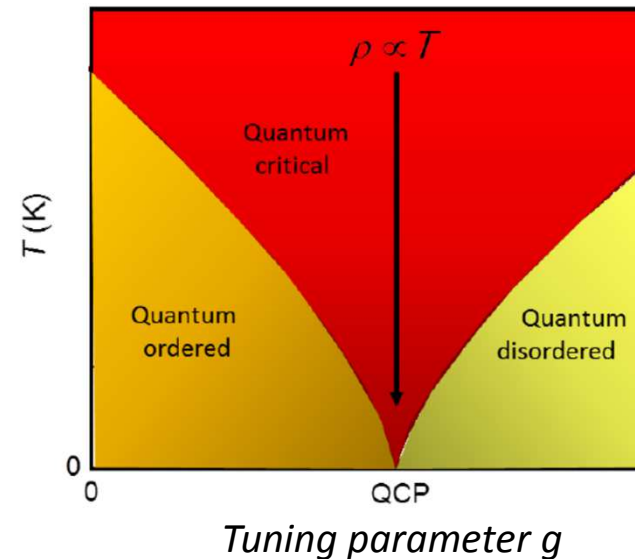
# Quantum criticality

## 'Classical' phase transition



Melting of ice = increase in thermal motion of the molecules as  $T$  is raised

## Quantum phase transition



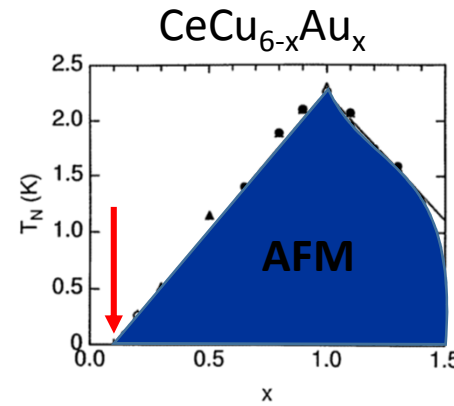
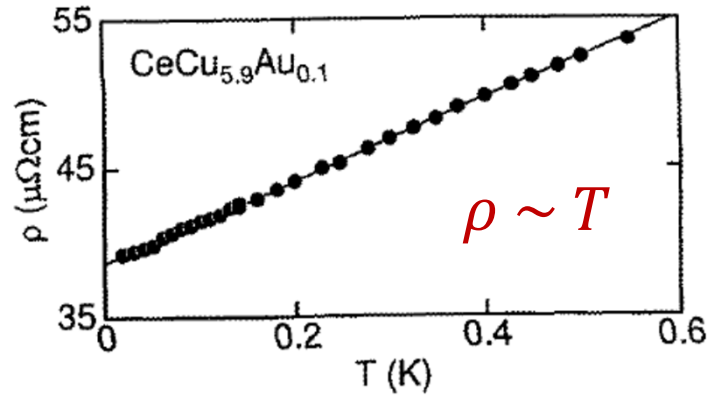
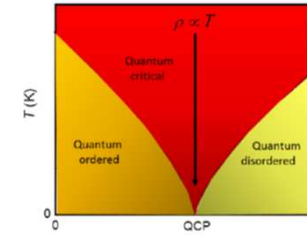
Phase transition that is driven not by  $T$  but by quantum fluctuations ('zero point motion')

$$\Delta x \cdot \Delta p \geq \hbar$$

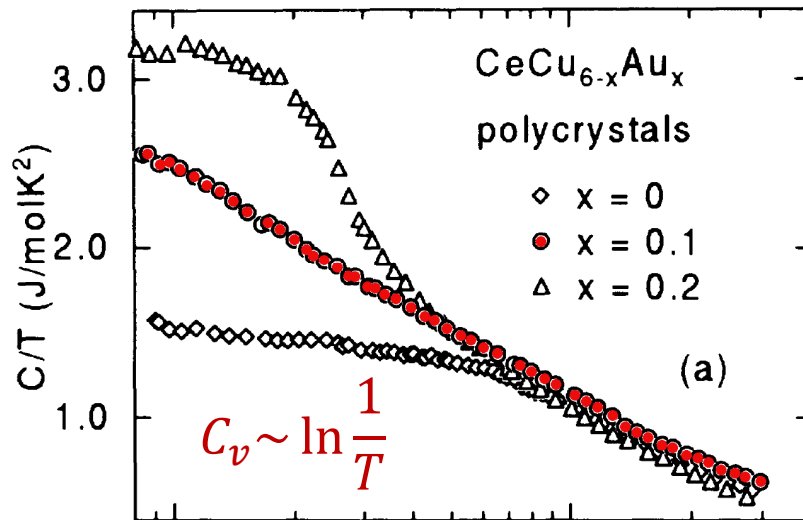
As  $T \rightarrow 0$ , thermal motion ceases but electron cannot be at rest ( $\Delta x$  and  $\Delta p$  fixed)

$\Rightarrow$  « State of constant agitation »  
that can melt order

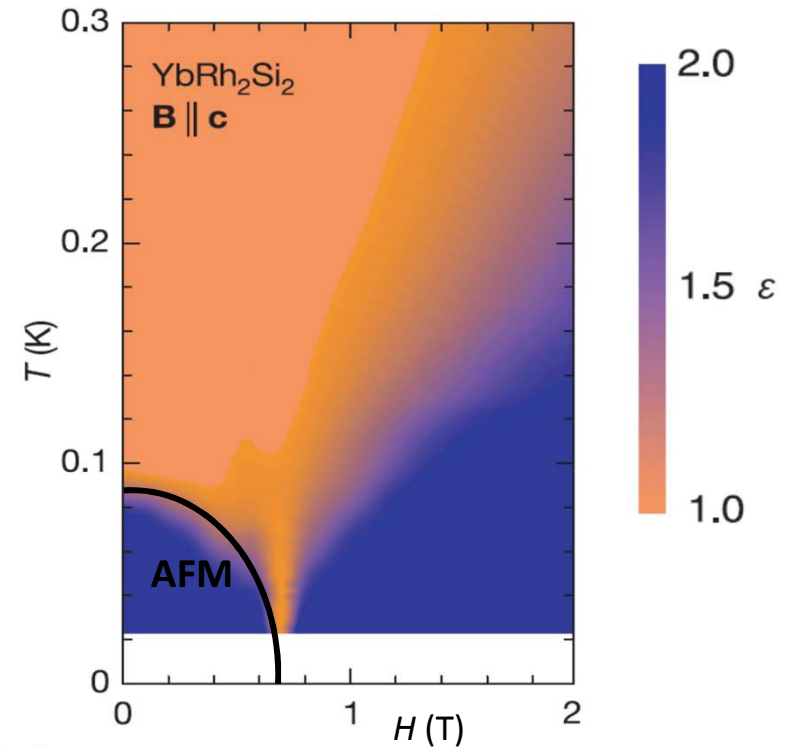
# Quantum critical metals



Lohneysen, *JPCM* 8 9689 (1996)



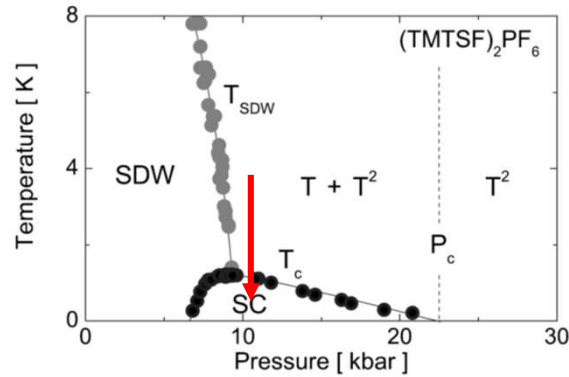
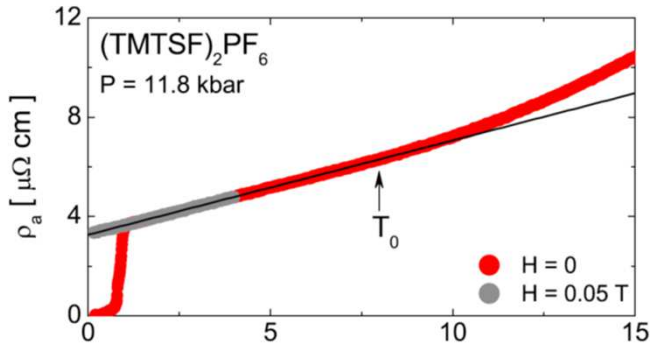
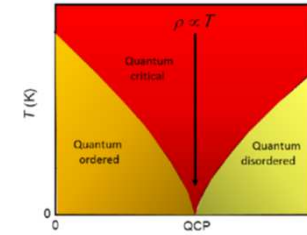
$C_v \sim m^* \Rightarrow m^* \rightarrow \infty$  at a QCP !



Custers *et al.*,  
*Nature* 424 524 (03)  $\rho = \rho_0 + A' T^\epsilon$

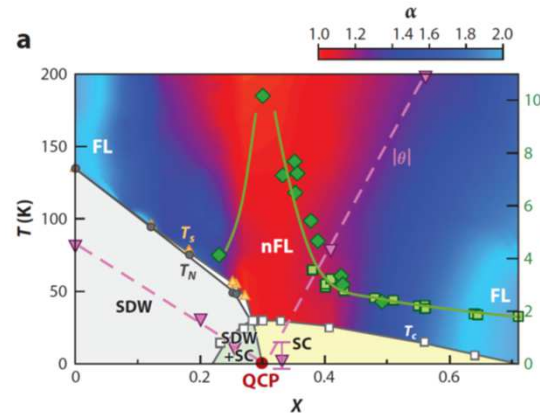
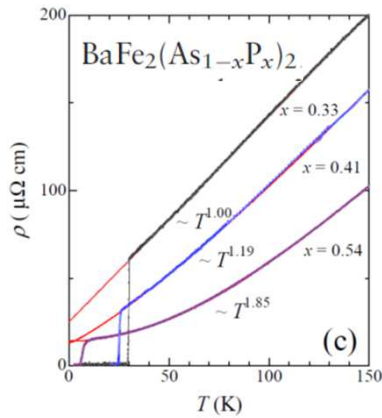


# Quantum critical metals



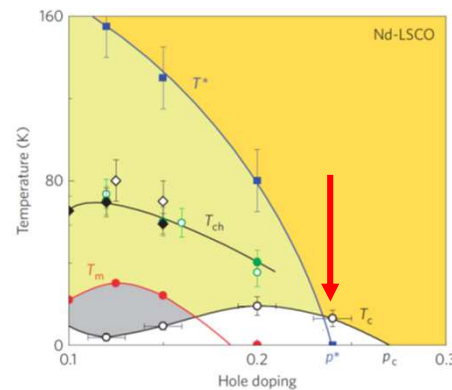
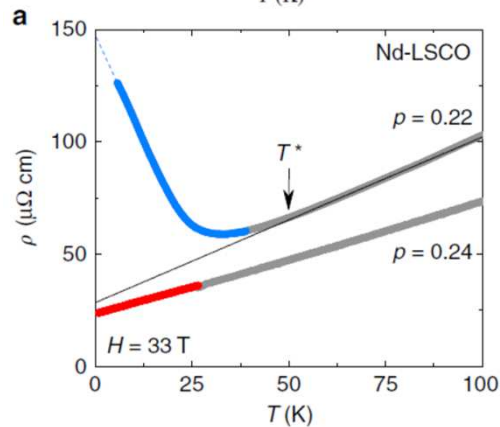
## Organic superconductors

Doiron-Leyraud *et al*,  
*PRB* **80** 214531 (2009)



## Pnictides

Shibauchi *et al*,  
*ARCMP* **5** 1113 (2014)



## Cuprates

Daou *et al*,  
*Nature Phys.* **5** 31 (2009)

# Origin of the $T$ -linear resistivity

VOLUME 82, NUMBER 21

PHYSICAL REVIEW LETTERS

24 MAY 1999

Interplay of Disorder and Spin Fluctuations in the Resistivity near a Quantum Critical Point

A. Rosch

$\rho \sim T$

Competition of weak, but isotropic impurity scattering and strong scattering from spin-fluctuations

PHYSICAL REVIEW B

VOLUME 51, NUMBER 14

1 APRIL 1995-II

Resistivity as a function of temperature for models with hot spots on the Fermi surface

R. Hlubina\* and T. M. Rice

**BUT**

Only effective at "hot spots" on the FS connected by the AF wavevector !  
The rest of the FS short-circuit the anomalous transport and yield  $\rho \sim T^2$

**Locally critical quantum phase transitions in strongly correlated metals**

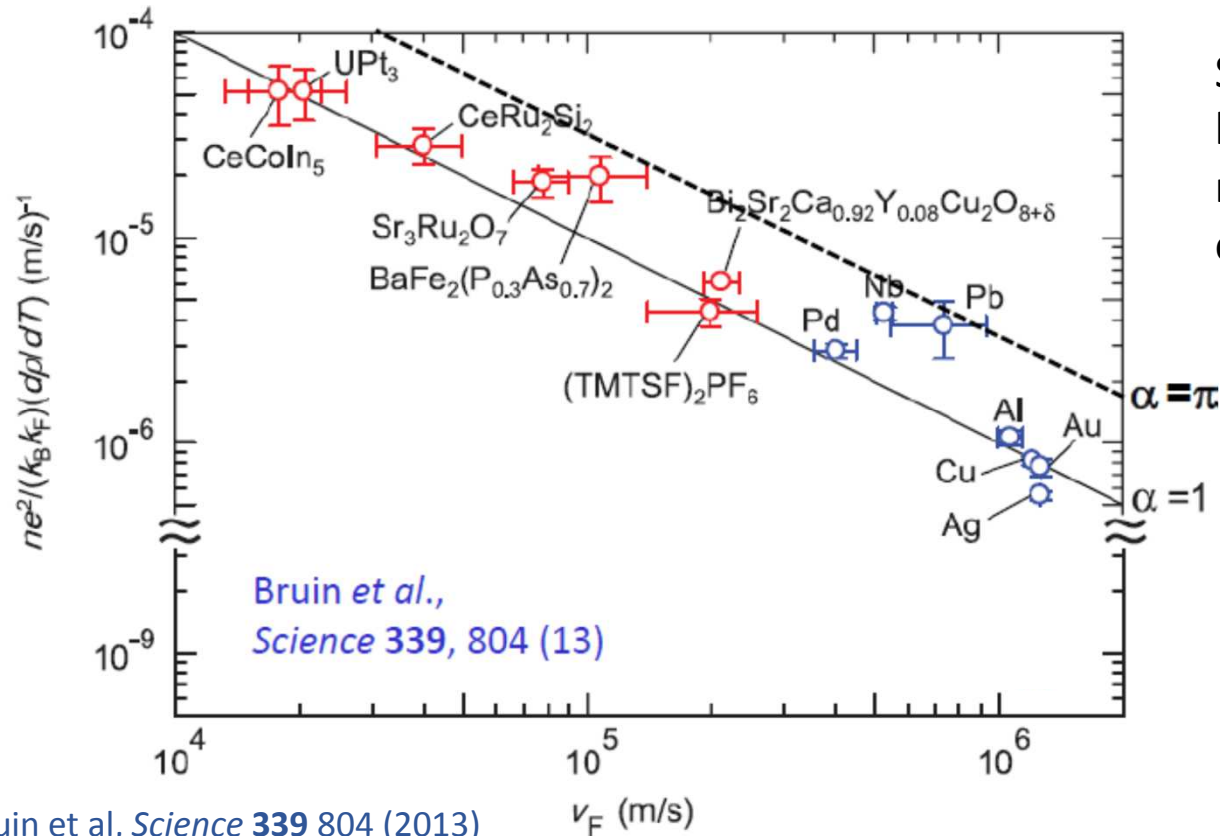
Qimiao Si\*, Silvio Rabello\*, Kevin Ingersent† & J. Llewellyn Smith\*

Nature 413,804 (2001)

Proposition: scattering near a QCP have a local character, i.e. no  $k$ -dependence  
 $\Rightarrow$  the entire FS is "hot" : Marginal Fermi liquid with  $\rho \sim T$

# Origin of the T-linear resistivity

## Planckian dissipation



Similar scattering rate per kelvin of metals in which resistivity is linear in T (QCP or e-ph scattering)

$$\hbar/\tau \sim \alpha k_B T$$

T is the only relevant energy scale

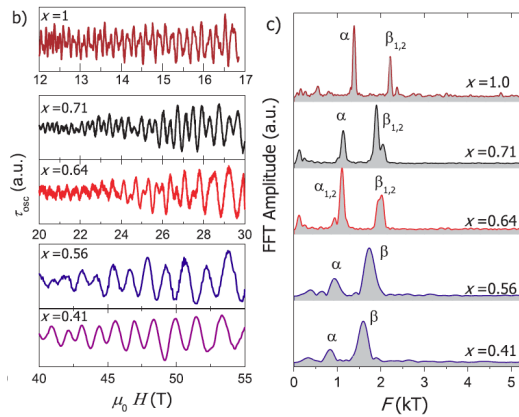
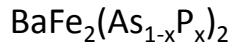
For SCES,  $0.9 < \alpha < 2.2$  in spite of differences in dimensionality and microscopic nature of the interactions.

The law of quantum mechanism forbids the dissipation time to be any shorter than  $\tau$

## 4. *High fields transport properties*

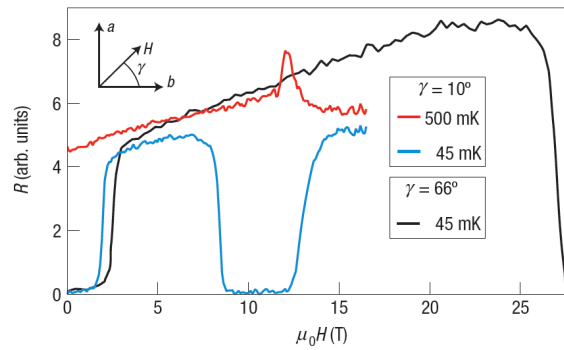
# Why high magnetic field ?

## RESOLVE FERMIOLGY



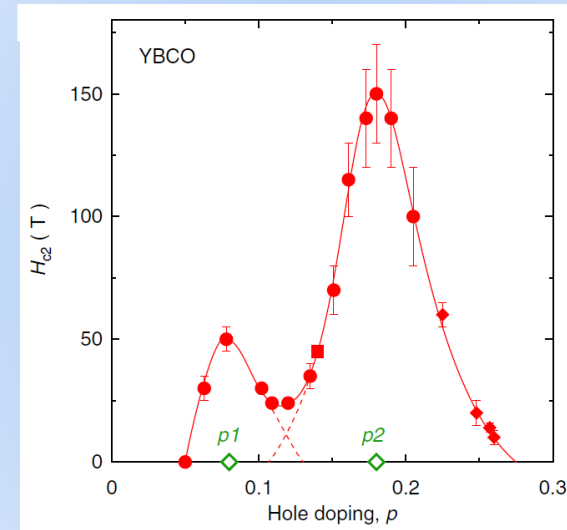
H. Shishido *et al.* PRL **104**, 057008 (2010)

## INDUCE NEW STATES OF MATTER & NEW PROPERTIES



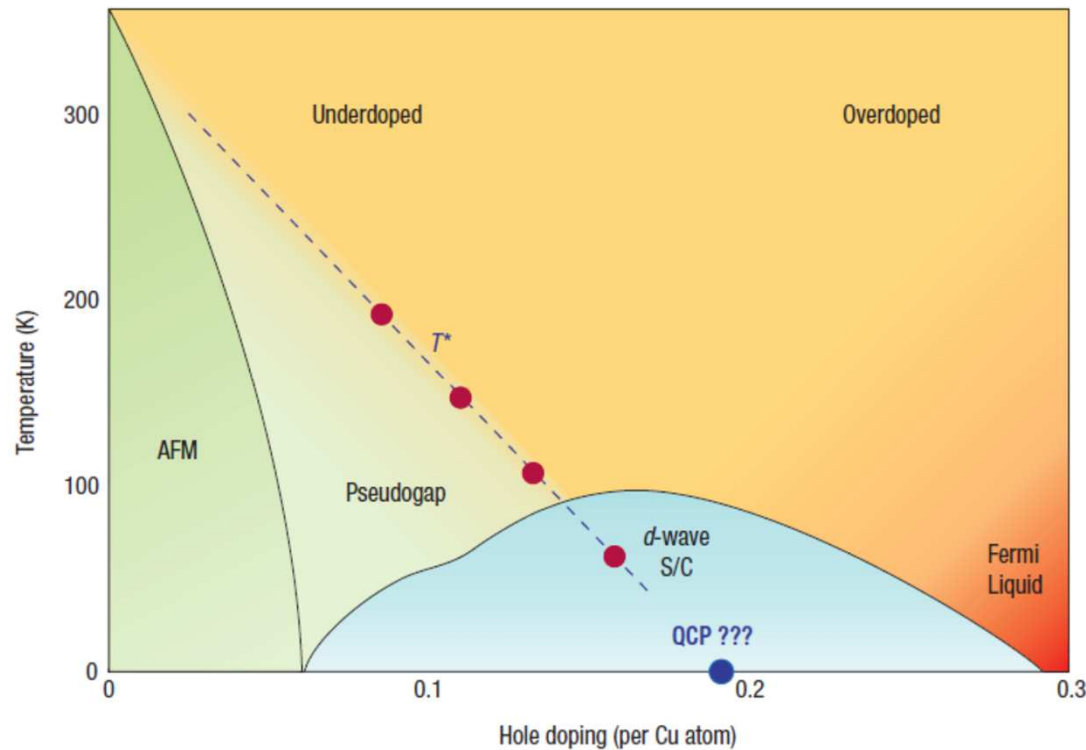
F. Lévy *et al.* Nature Phys. **3**, 460 (2007)

## RESTORE THE NORMAL STATE OF SUPERCONDUCTORS



G. Grissonnanche *et al.* Nature Comm. **5**, 3280 (2014)

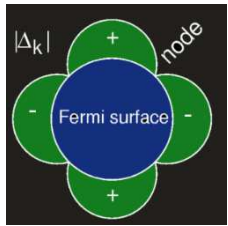
# Pseudogap and quantum criticality in cuprates



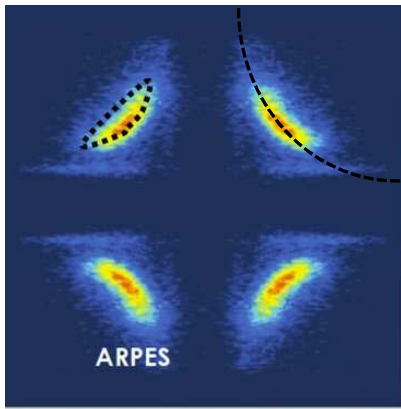
« Although it is difficult to predict the role that quantum criticality will play in our final understanding of the cuprates, the case for a QCP would be made very compelling if a new experiment were to reveal a sharp and pronounced change in some electronic property in the zero-temperature limit, on crossing the QCP as a function of doping. »

Broun, *Nature Physics* 4 170 (2008)

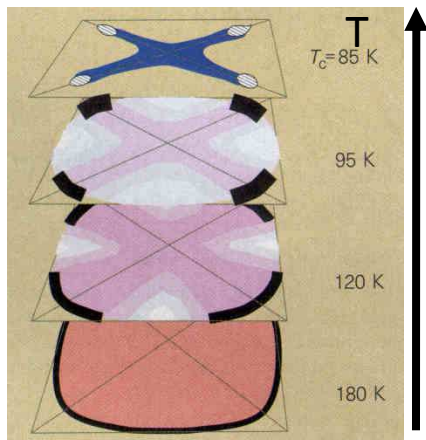
# Pseudogap and quantum criticality in cuprates



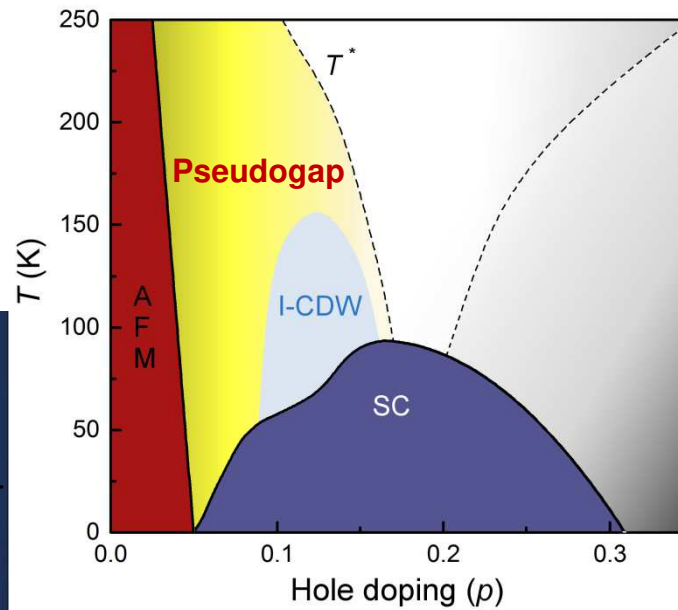
ARPES



adapted from Hossain *et al*/Nature Phys. 2008



M. Norman *et al*, Nature'98

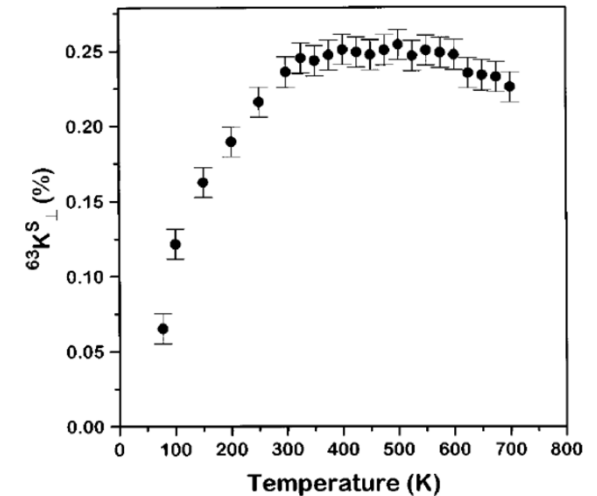


Partial suppression of the low energy excitation as seen by spectroscopy and thermodynamic probes and located at the anti-node

Doped Mott insulator ?

Phase with a distinct order parameter?

NMR: Pseudogap for  $T < T^*$  (crossover)

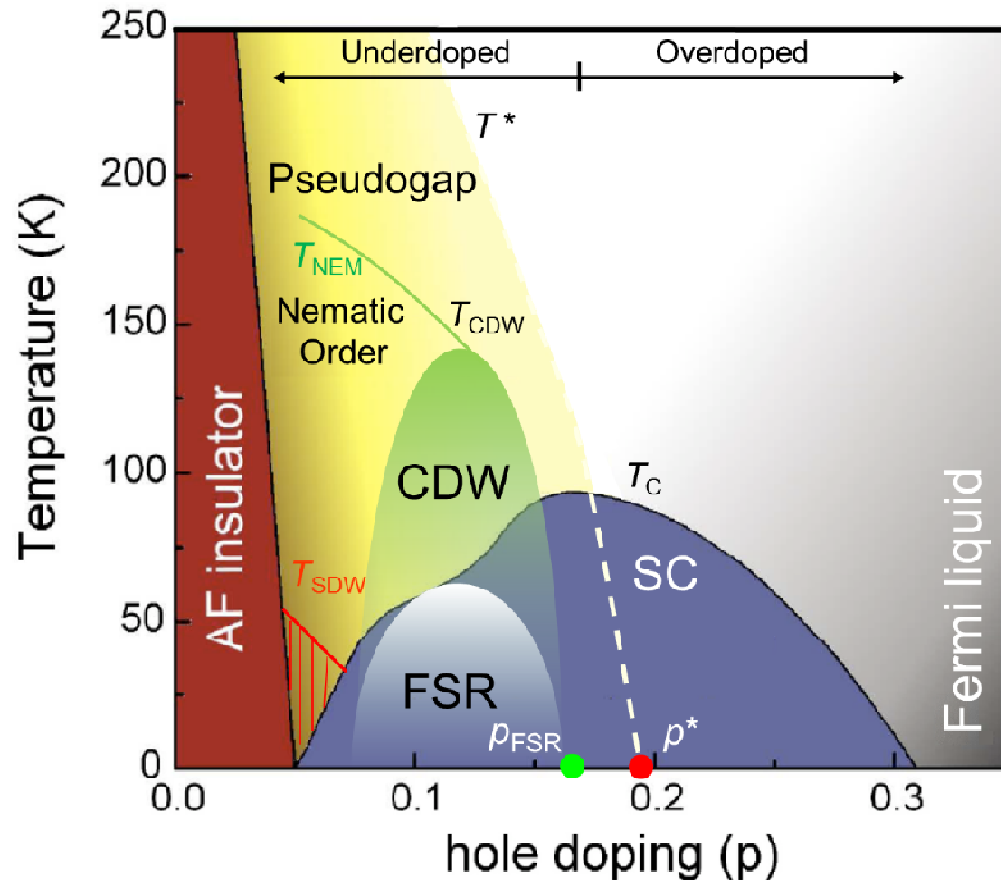


Curro *et al*, PRB 56, 877 (1997)

$$K \propto \chi'(q=0, \omega) \propto \text{DOS}$$

# Pseudogap and quantum criticality in cuprates

Pseudogap = partial suppression of the low energy excitation as seen by spectroscopy and thermodynamic probes and located at the anti-node (from ARPES)



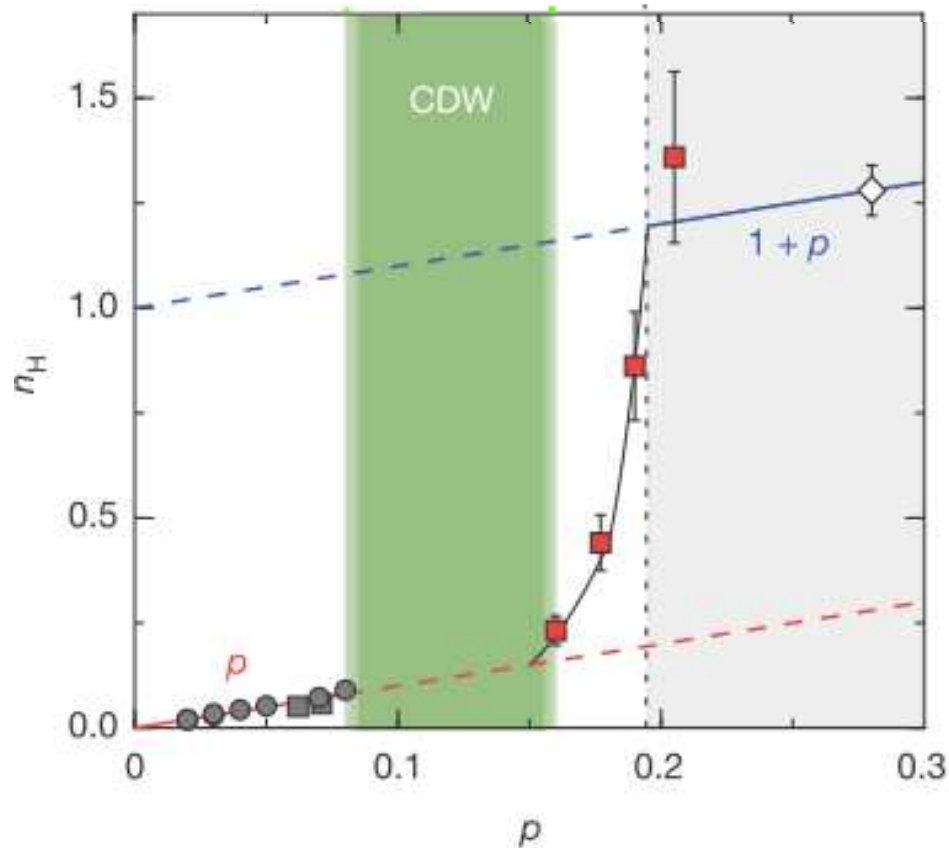
- ✓ Orbital current
  - ✓ Nematic
  - ✓ ~~CDW~~
  - ✓ AF ?
- } Q=0

**The broken symmetries are instability of the pseudogap**

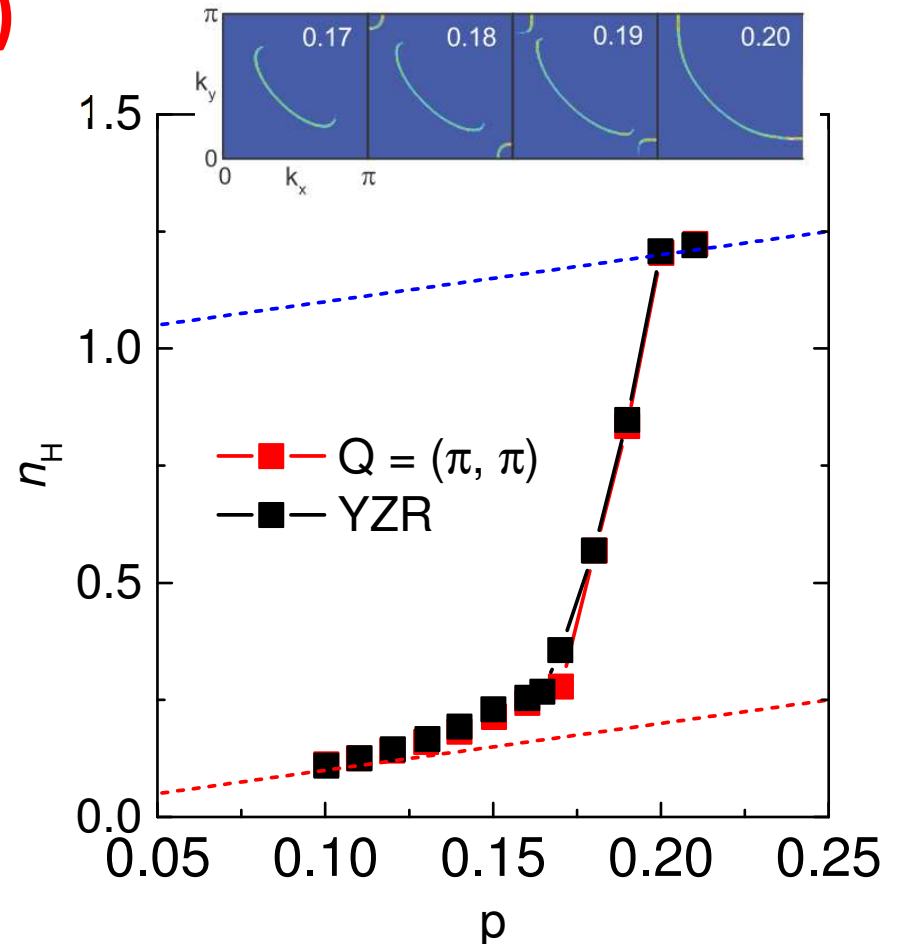


# Pseudogap and quantum criticality in cuprates

Low T ( $H = 80$  T)



S. Badoux *et al.*, Nature (2016)



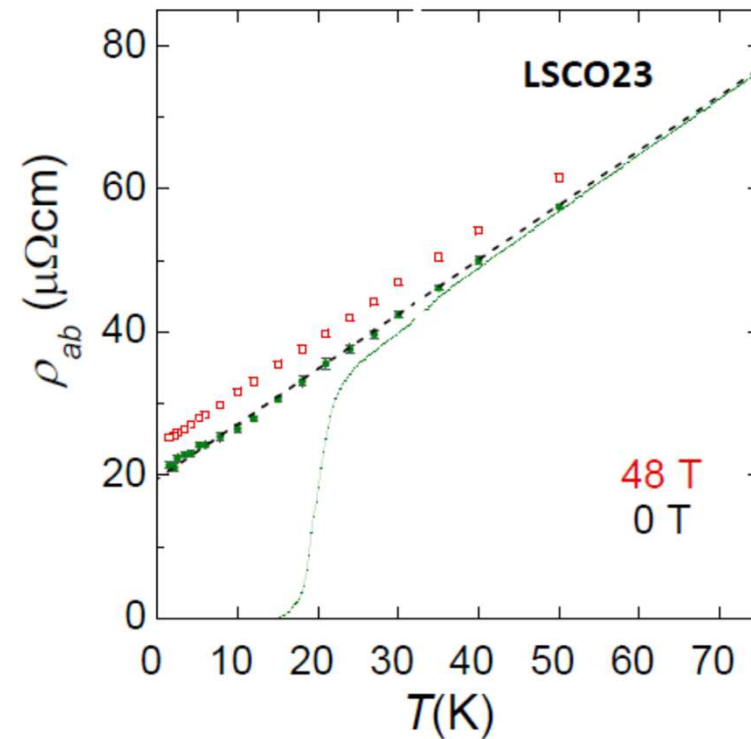
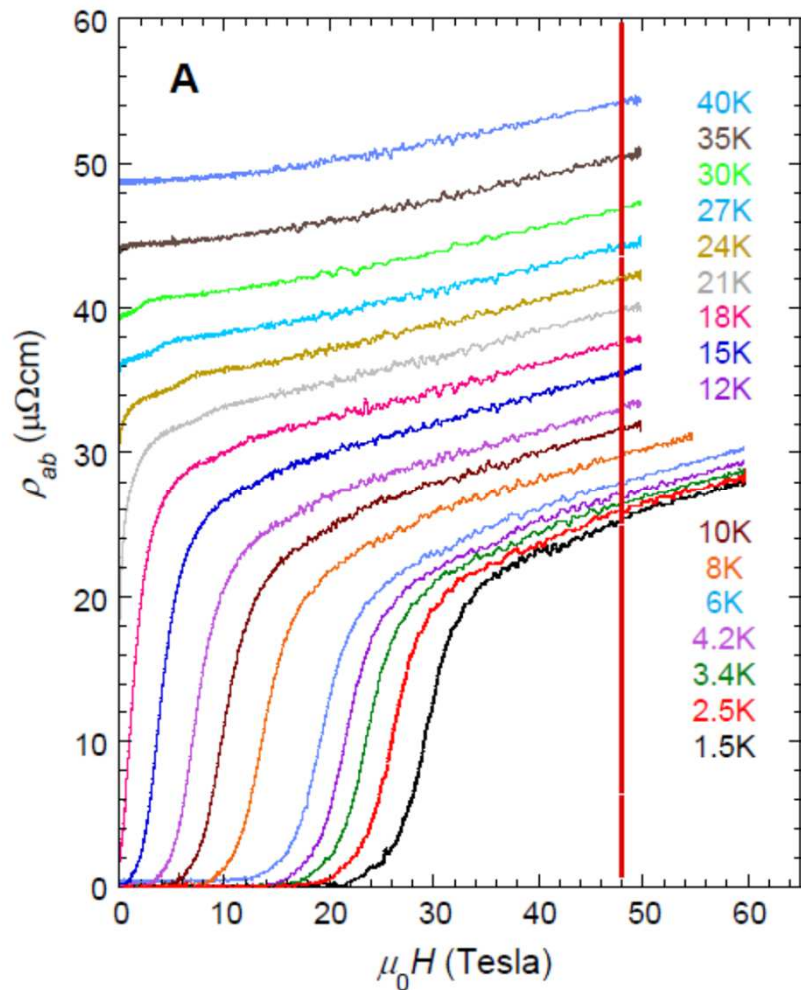
J.G. Storey *et al.*, Euro. Phys. Lett. (2016)

- Pseudogap and charge order are separate phenomena.
- Sharp drop of the carrier density at the critical point of the pseudogap.

# High fields transport properties in LSCO

Access ground state using pulsed magnetic fields

**T-linear term** becomes dominant at low  $T$

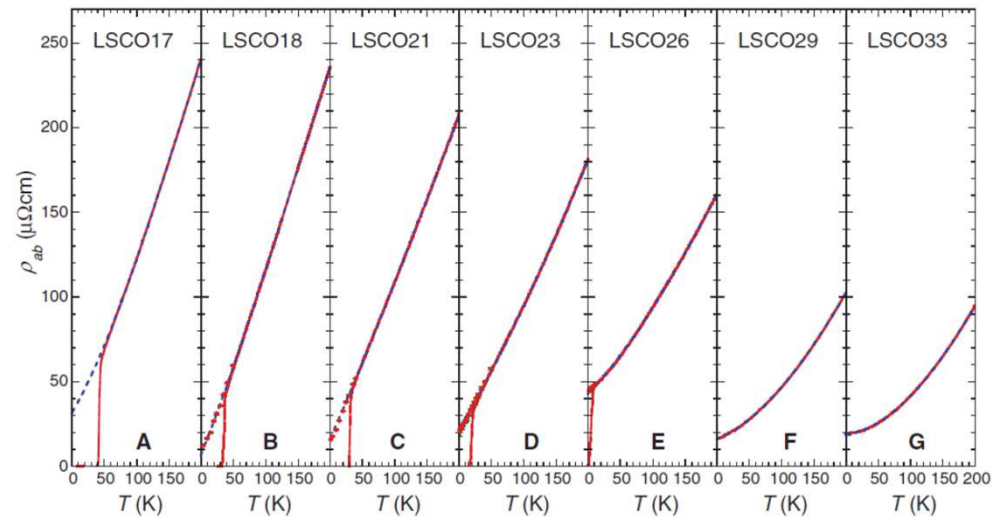


Cooper et al., *Science* **323**, 603 (2009)

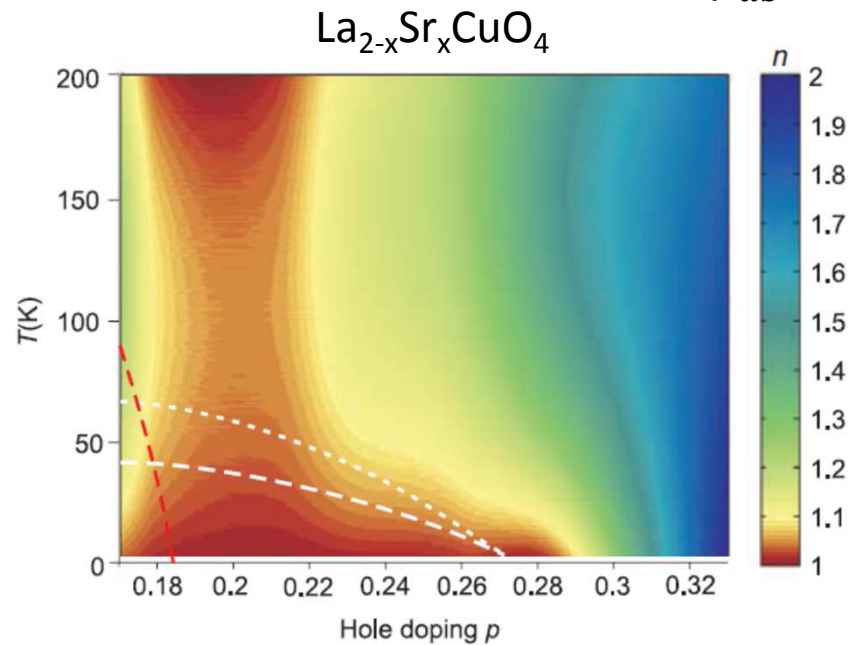
# Anomalous criticality in LSCO

Cooper *et al.*, *Science* **323**, 603 (2009)

$\rho_{ab}(T)$  remains  $T$ -linear at low  $T$  over an anomalously wide doping range



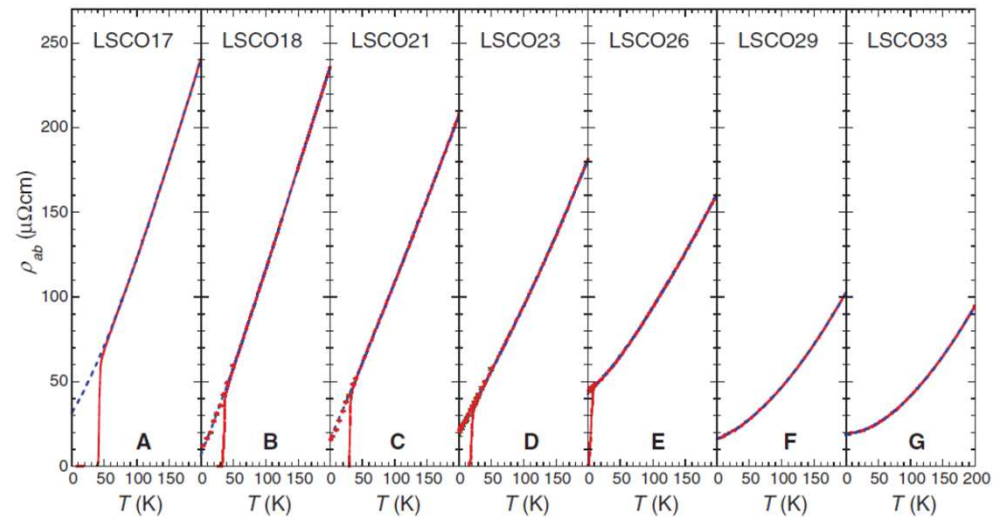
$$\Delta\rho_{ab}(T) = \alpha_n T^n$$



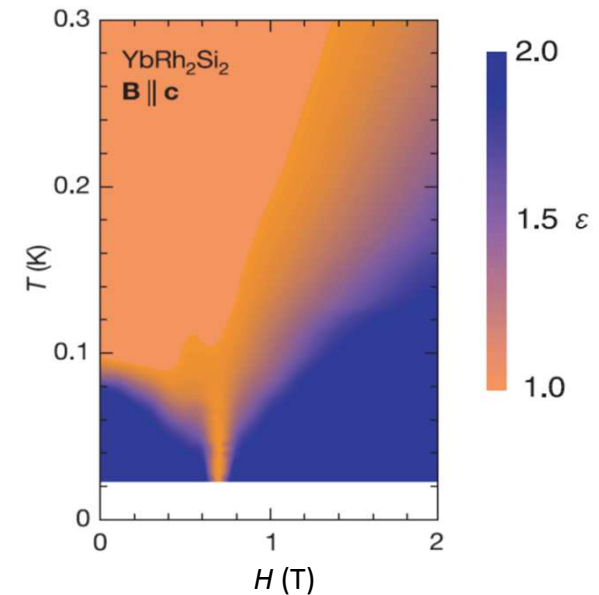
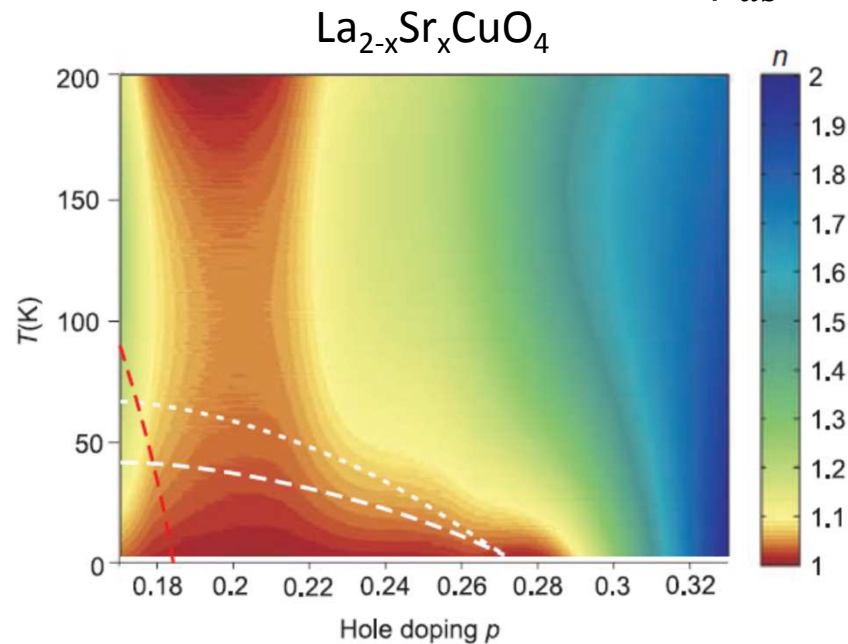
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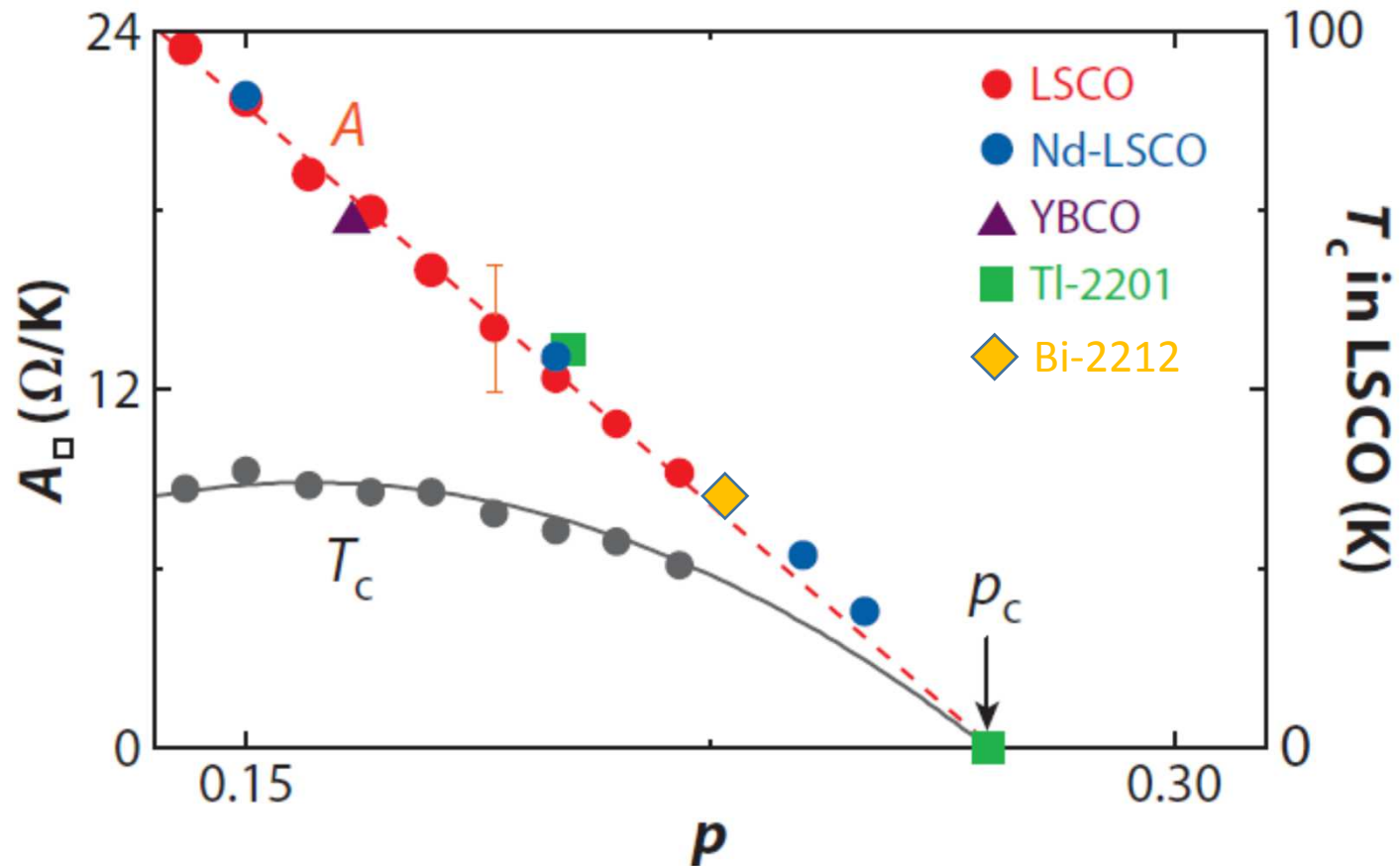


$$\Delta\rho_{ab}(T) = \alpha_n T^n$$



# Discussion

Doping dependence of the linear term of the resistivity in hole-doped cuprates



**“What scatters may also pair”**

Taillefer, *ARCOMP* 1, 51 (2010)